



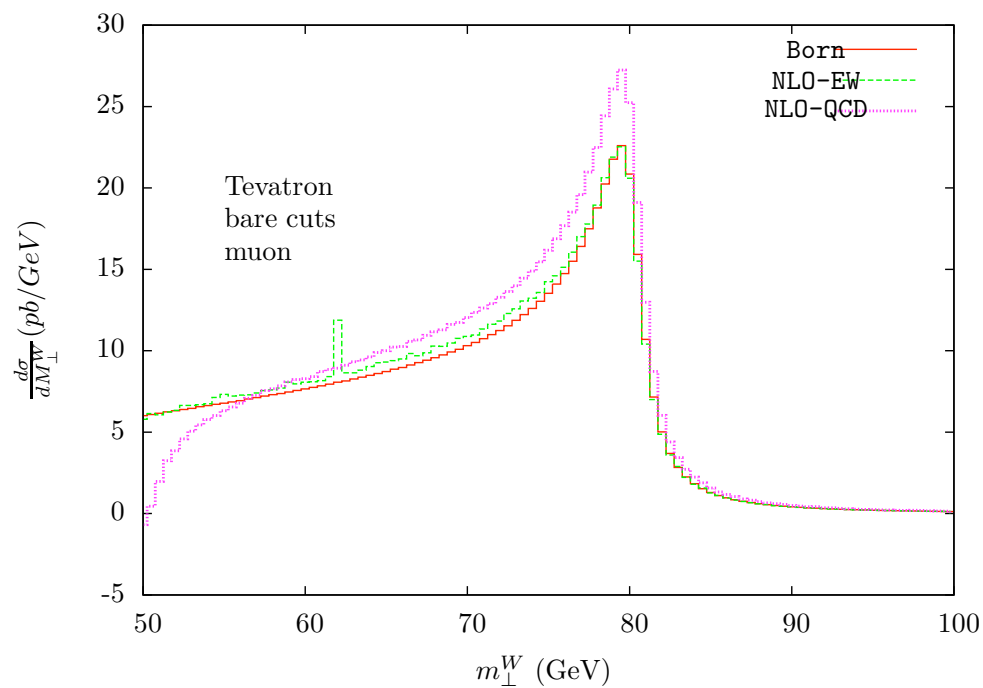
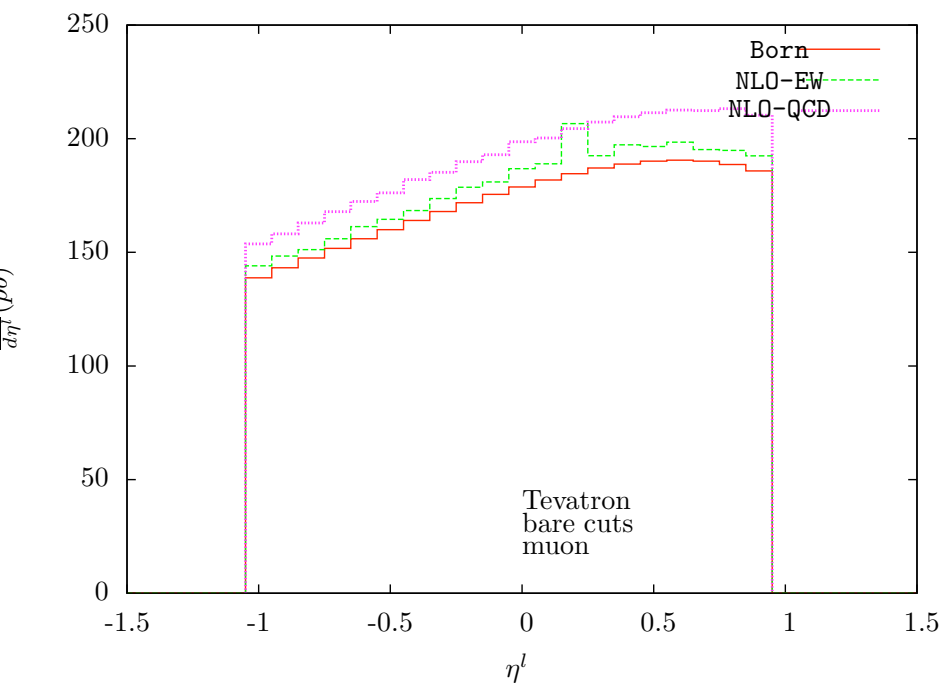
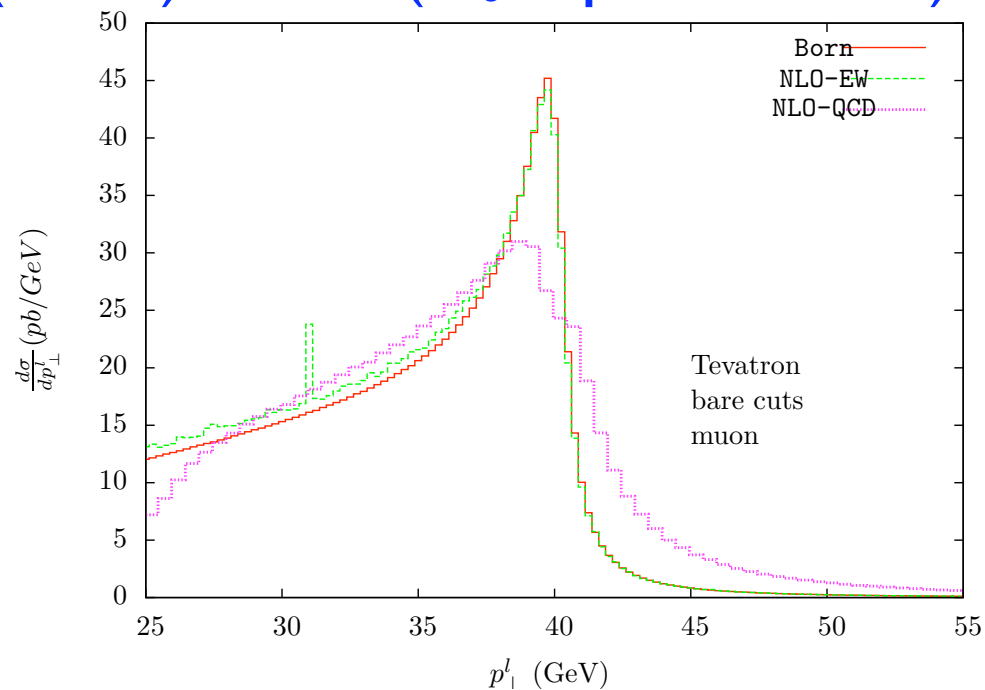
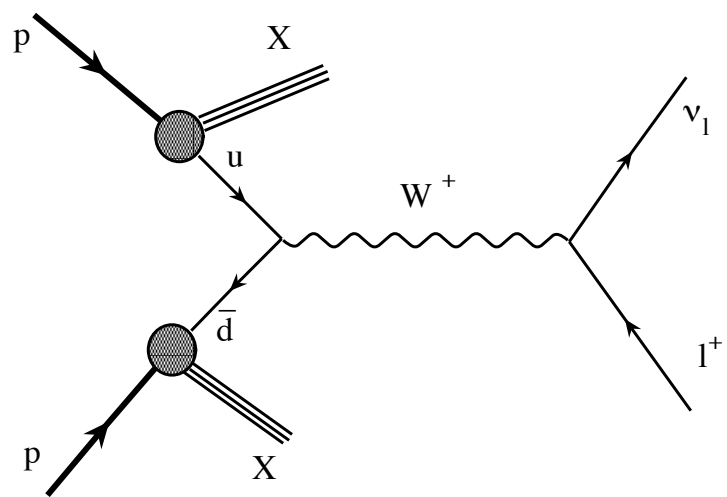
# EW higher order corrections and EW scheme uncertainties: a fitting exercise

**Alessandro Vicini**  
University of Milano, INFN Milano

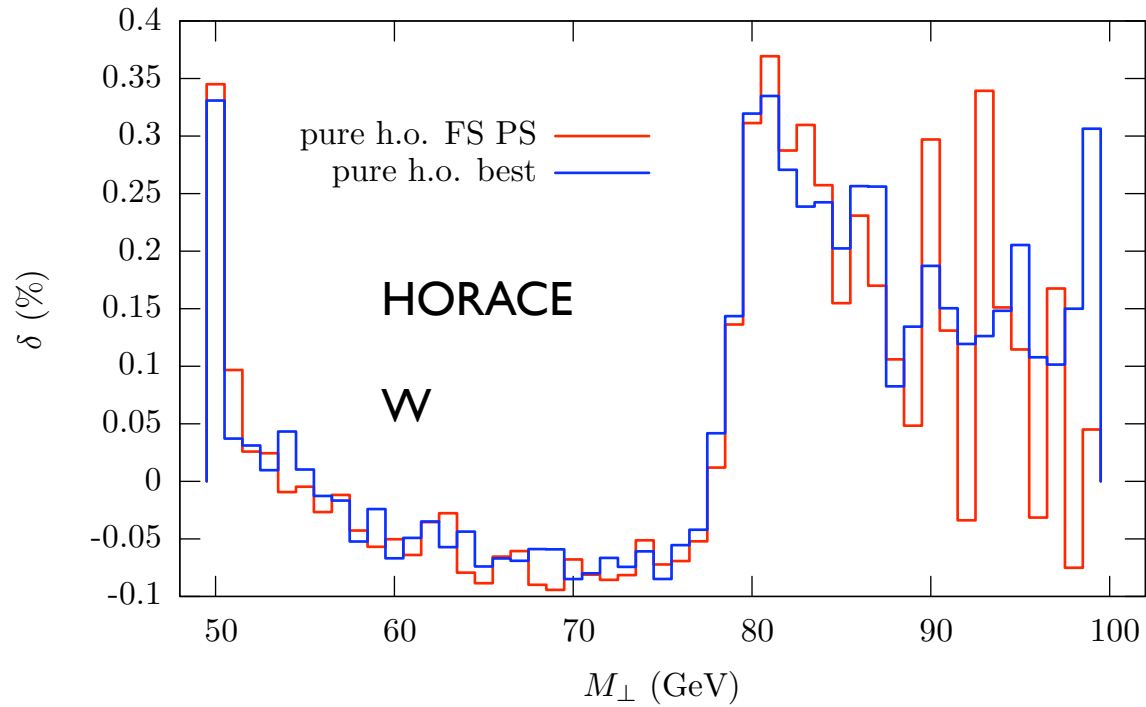
W mass workshop  
Fermilab, October 5th 2010

in collaboration with C.M.Carloni Calame

# The Drell-Yan process at fixed (NLO) order ( $\alpha_0$ input scheme)



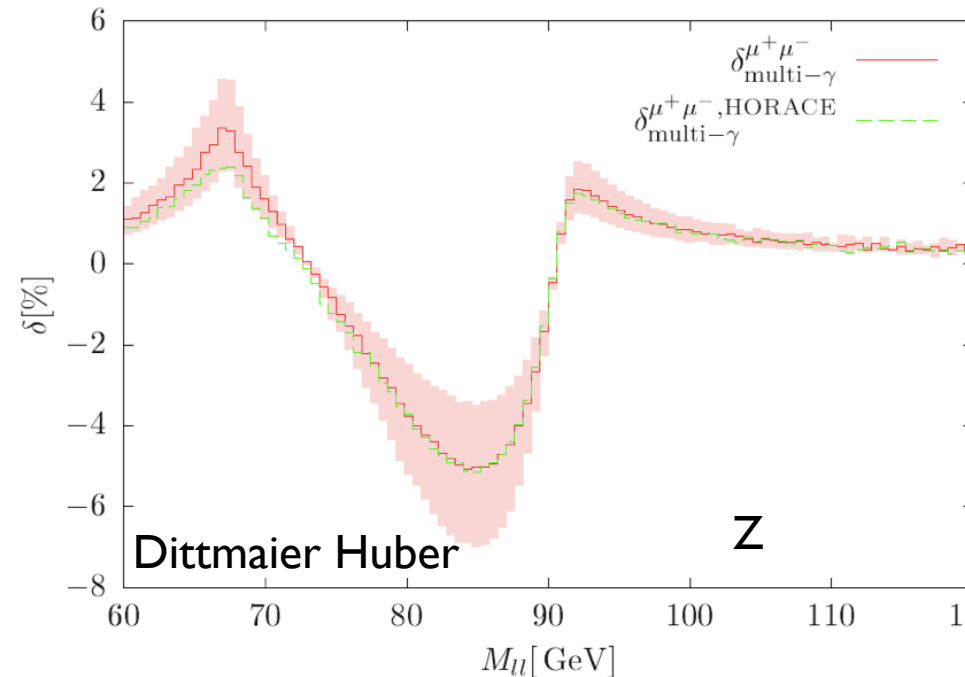
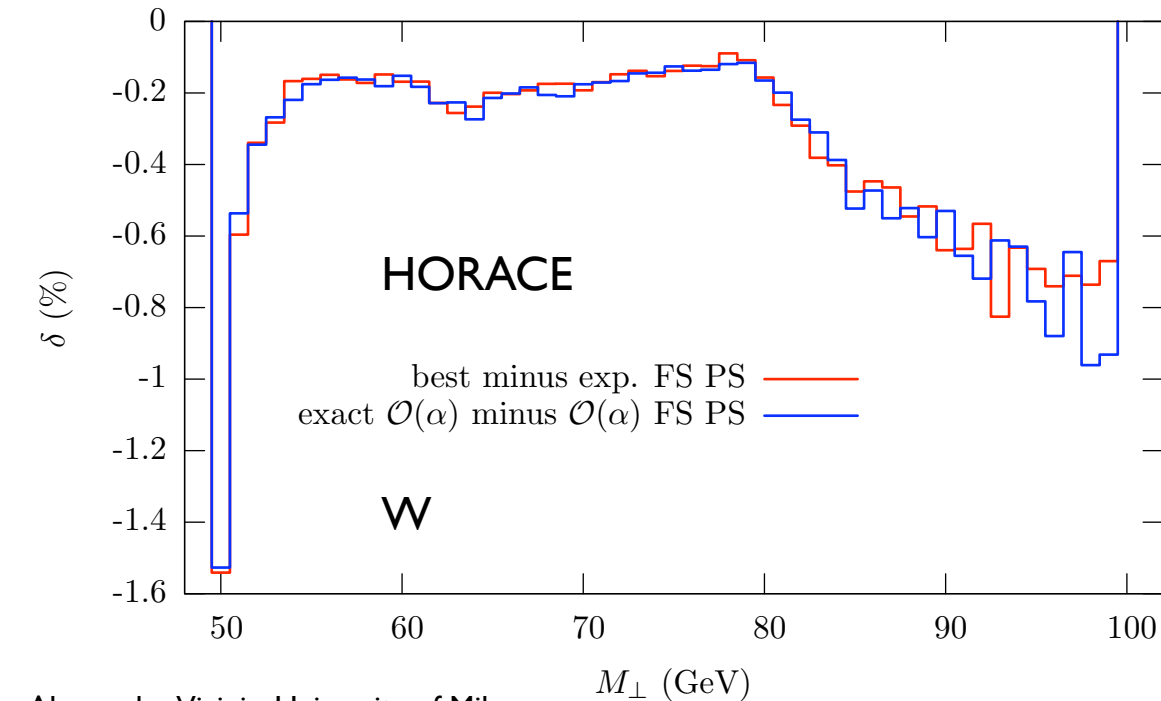
# The effect of multiple photon emission and of subleading EW terms



Effects of multiple photon emission studied

HORACE : full all orders QED Parton Shower

W-ZGRAD, Dittmaier-Huber:  
final state structure function approach



# The W mass as pseudo-observable

The **W mass** is not a property of measured (final state) particles, but it is rather an **input parameter of the Lagrangian** which can be chosen to maximize the agreement theory-data for some given distributions.

If we want to measure  $M_W$ , in the SM, in the gauge sector, it is possible to use as inputs  
 $(\alpha, m_W, m_Z)$      $(G_\mu, m_W, m_Z)$     but not     $(\alpha, G_\mu, m_Z)$

The W mass is defined starting from the pole, in the complex plane, of the W propagator

Since the final state neutrino escapes detection, it is not possible to reconstruct all the components of the W momentum (and therefore its virtuality).

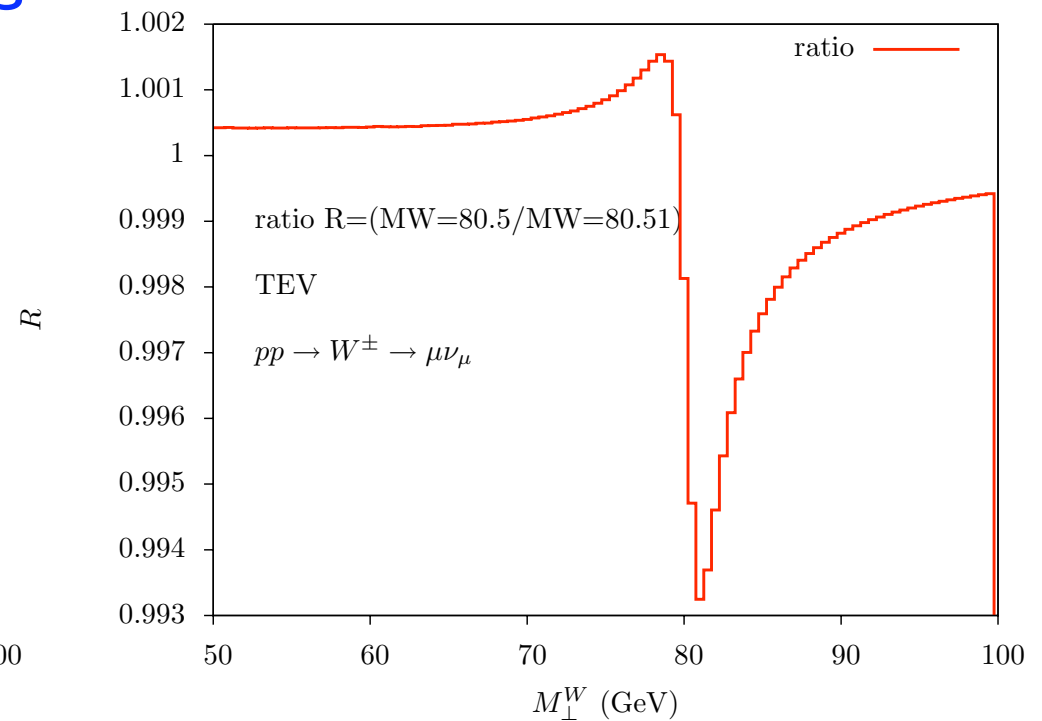
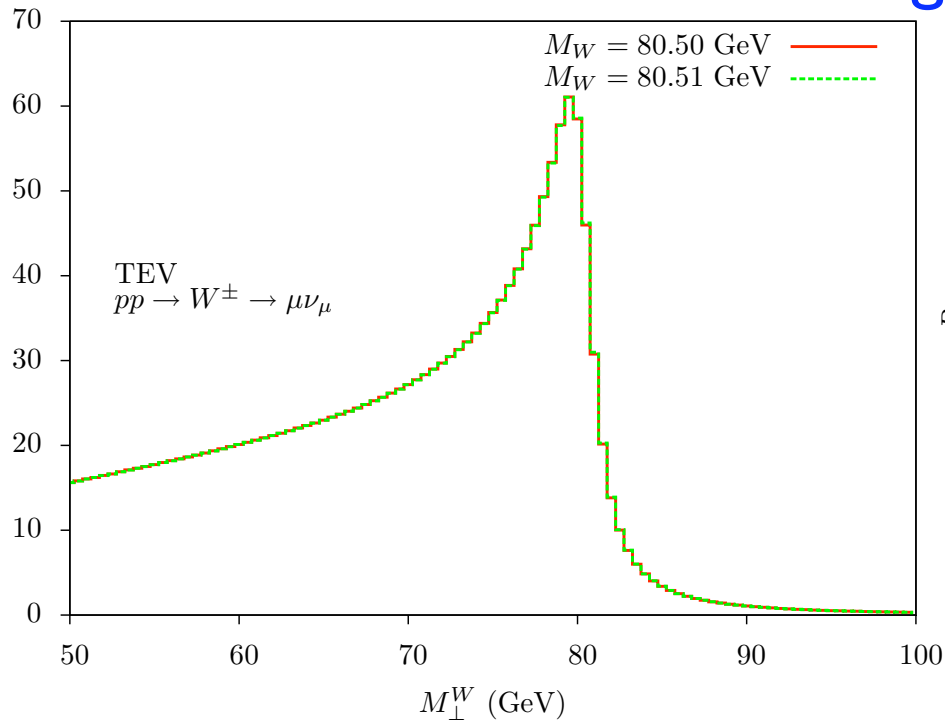
It is possible to infer the value of the **transverse components of the neutrino** **provided one has an excellent understanding of initial state QCD+QED radiation**

The lepton and the missing transverse momentum and transverse mass distributions have a jacobian peak about the W mass.

The peak of distributions provides a strong sensitivity to the value of  $M_W$ .

$$M_{\perp}^W = \sqrt{2p_{\perp}^l p_{\perp}^{\nu} (1 - \cos \phi_{l\nu})}$$

# Estimate of MW shift due to higher order corrections in the fit



The ratio of two distributions generated with nominal MW which differ by 10 MeV shows a deviation from unity at the level of few per mil, with non trivial shape

If we aim at measuring MW with 10-15 MeV of error, are we able to control the **shape** of the distributions and the theoretical uncertainties at the **few per mil level**?

Not all the radiative corrections have the same impact on the MW measurement  
not all the uncertainties are equally bad on the final error

# The template-fitting procedure

A distribution computed with a given set of radiative corrections and with a given value  $MW_0$  is treated as a set of pseudo-data

The templates are prepared in Born approximation, using 100 values of  $MW_i$ . Each template is compared to the pseudo-data and a distance is measured

$$\chi_i^2 = \sum_{j=1}^{N_{bins}} \frac{\left(O_j^{data} - O_j^{templ=i}\right)^2}{\left(\sigma_j^{data}\right)^2} \quad i = 1, \dots, N_{templ}$$

The template that minimizes the distance is considered as the “preferred one” and the value of  $MW$ , used to generate it, is the “measured”  $MW$

The difference  $MW - MW_0$  represents the shift induced on the measurement of the  $W$  mass by including that specific set of radiative corrections

The distributions used in the evaluation of  $\chi_i^2$  in general do not have the same normalization. It is also possible to compare distributions that have been normalized to their respective xsecs, to appreciate the role of the shape differences

# The HORACE formula:

exact  $O(\alpha)$  matched with multiple photon radiation

$$d\sigma_{\text{matched}}^{\infty} = \Pi_S(Q^2) F_{SV} \sum_{n=0}^{\infty} d\hat{\sigma}_0 \frac{1}{n!} \prod_{i=0}^n \left( \frac{\alpha}{2\pi} P(x_i) I(k_i) dx_i d\cos\theta_i F_{H,i} \right)$$

$$F_{SV} = 1 + \frac{d\sigma_{SV}^{\alpha,ex} - d\sigma_{SV}^{\alpha,PS}}{d\sigma_0}$$

$$F_{H,i} = 1 + \frac{d\sigma_{H,i}^{\alpha,ex} - d\sigma_{H,i}^{\alpha,PS}}{d\sigma_{H,i}^{\alpha,PS}}$$

The matched HORACE formula is based on the all-orders QED Parton Shower structure

The presence of the overall Sudakov form factor guarantees the “semi-classical” limit  
The Sudakov form factor contains the (IR) LL virtual corrections

The exact  $O(\alpha)$  accuracy is reached by adding

**finite** (no IR-div) soft+virtual effect in the overall factor  $F_{SV}$

**exact** (vs. eikonal) hard matrix element effects to every photon emission  $F_{H,i}$

## EW input schemes

$$\frac{G_\mu}{\sqrt{2}} = \frac{g^2}{8m_W^2} (1 + \Delta r)$$
$$\alpha_\mu^{tree} = \frac{\sqrt{2}}{\pi} G_\mu m_W^2 \sin^2 \theta_W$$
$$\alpha_\mu^{1l} = \frac{\sqrt{2}}{\pi} G_\mu m_W^2 \sin^2 \theta_W (1 - \Delta r)$$

$$\alpha_0 : \quad \sigma = \alpha_0^2 \sigma_0 + \alpha_0^3 (\sigma_{SV} + \sigma_H)$$
$$G_\mu \text{ I} : \quad \sigma = (\alpha_\mu^{tree})^2 \sigma_0 + (\alpha_\mu^{tree})^2 \alpha_0 (\sigma_{SV} + \sigma_H) - 2\Delta r (\alpha_\mu^{tree})^2 \sigma_0$$
$$G_\mu \text{ II} : \quad \sigma = (\alpha_\mu^{1l})^2 \sigma_0 + (\alpha_\mu^{1l})^2 \alpha_0 (\sigma_{SV} + \sigma_H)$$

the three input schemes differ by  $O(\alpha^2)$  terms

the change of scheme yields a different overall normalization

but also

the sharing of 0- and of 1-photon events is different in the 2  $G_\mu$  schemes

the same in  $\alpha_0$  and  $G_\mu$ -II schemes



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the sharing of 0- and of **l-photon** events is different in the 2  $G_\mu$  schemes

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the three input schemes differ by  $O(\alpha^2)$  terms

the change of scheme yields a different overall normalization

but also

the sharing of 0- and of l-photon events is different in the 2 Gmu schemes

the same in  $\alpha_0$  and Gmu-II schemes

# The HORACE formula and its impact on the MW measurement

$$d\sigma_{matched}^{\infty} = \Pi_S(Q^2) F_{SV} \sum_{n=0}^{\infty} d\hat{\sigma}_0 \frac{1}{n!} \prod_{i=0}^n \left( \frac{\alpha}{2\pi} P(x_i) I(k_i) dx_i d\cos\theta_i F_{H,i} \right)$$

$$F_{SV} = 1 + \frac{d\sigma_{SV}^{\alpha,ex} - d\sigma_{SV}^{\alpha,PS}}{d\sigma_0} \quad F_{H,i} = 1 + \frac{d\sigma_{H,i}^{\alpha,ex} - d\sigma_{H,i}^{\alpha,PS}}{d\sigma_{H,i}^{\alpha,PS}}$$

in the matched HORACE formula **the change of input scheme** affects:

the overall couplings of the Born cross-section  $d\sigma_0$  and  
the  $F_{SV}$  factor

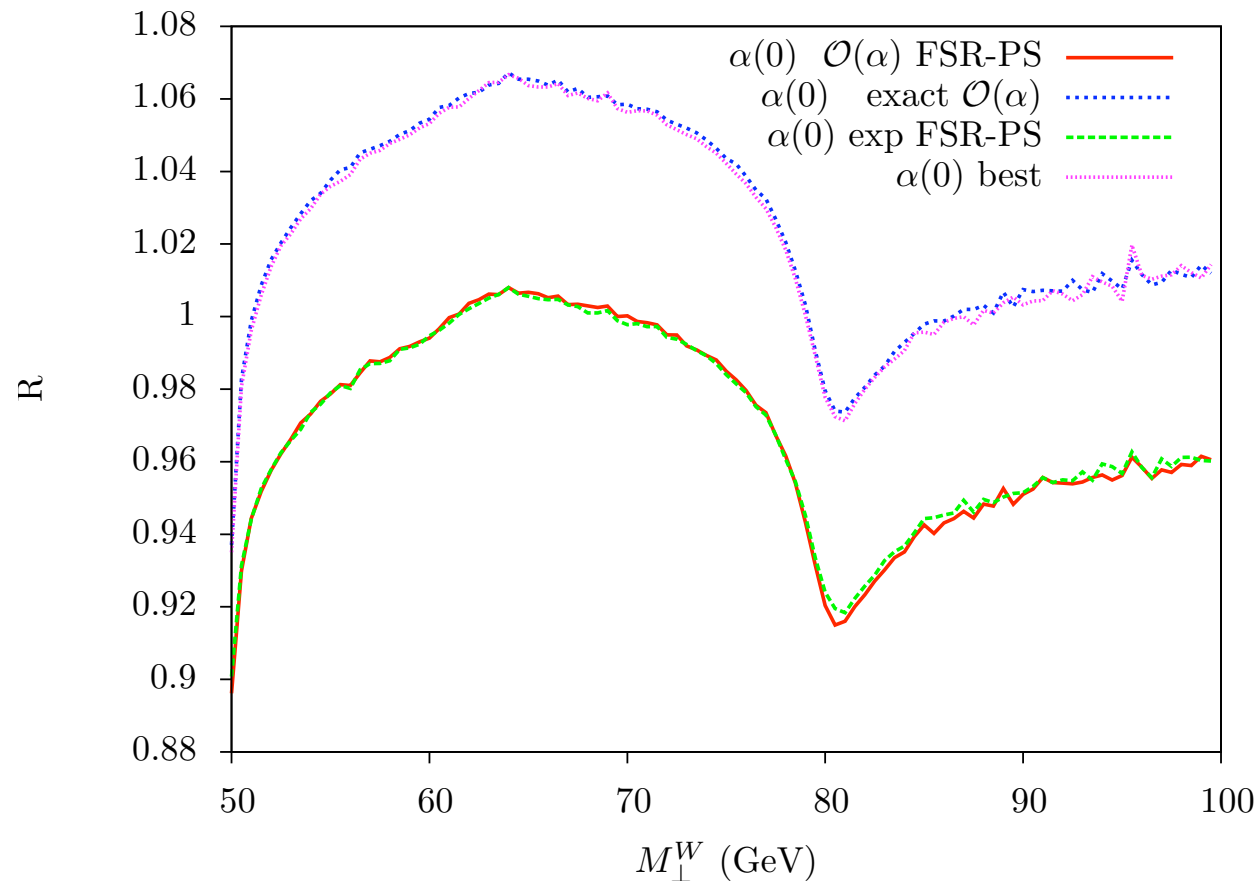
in both cases it **modifies the overall normalization** of the cross section

**the sharing of 0-, 1-, 2-,.... photon events remains the same** in **all the input schemes**  
and therefore the shape of the distributions (relevant for MW) remains the same

The input scheme changes differ at  $O(\alpha^2)$  and  
modify mostly the normalization of the cross section,

Therefore the  $\chi^2$  of the fit exhibits a corresponding variation.

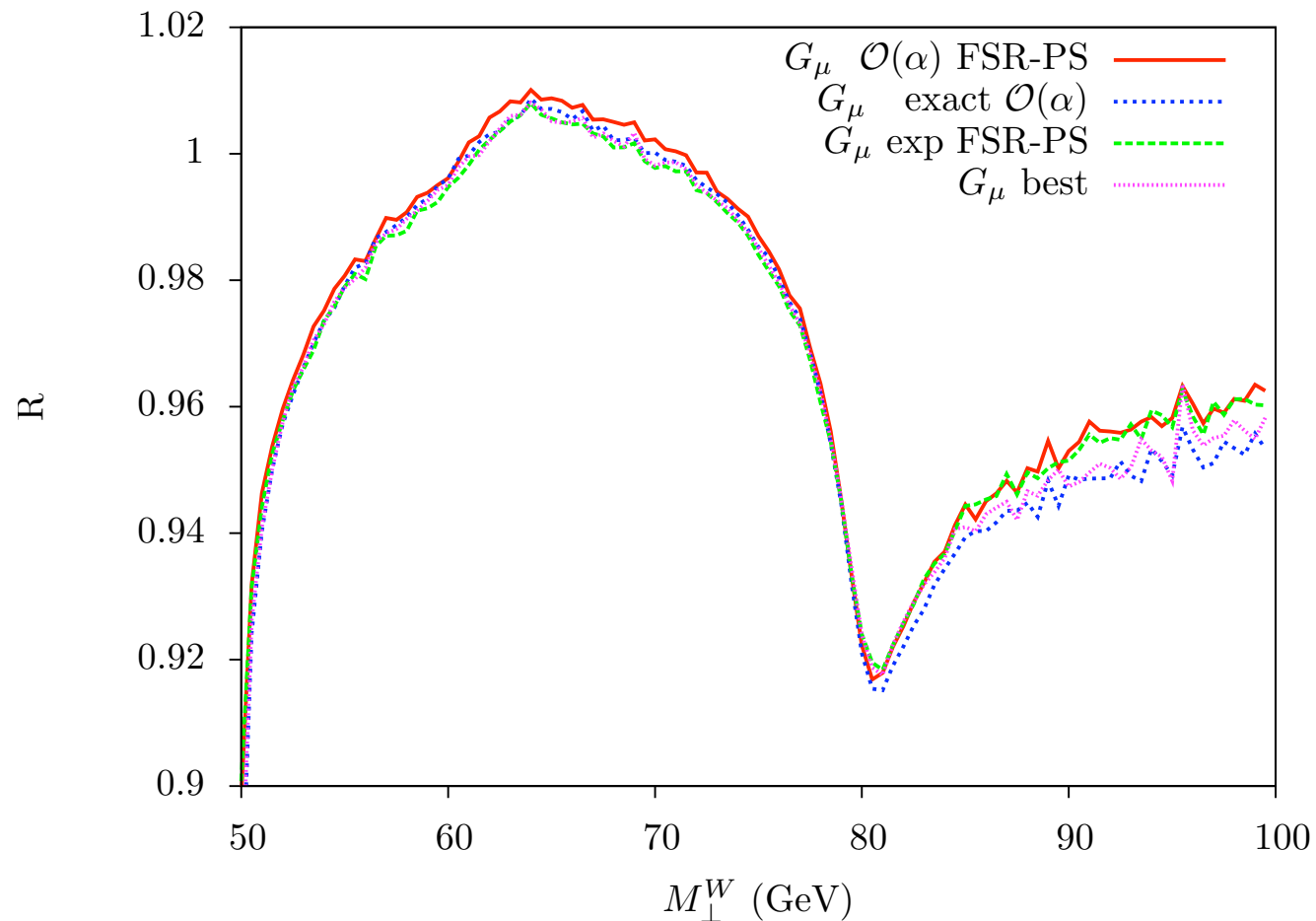
# EW higher orders in the $\alpha_0$ scheme: percentual effect (in unit Born)



The 2 lower curves are obtained with FSR QED Parton Shower

The 2 upper curves show the effect of the 1-loop virtual corrections

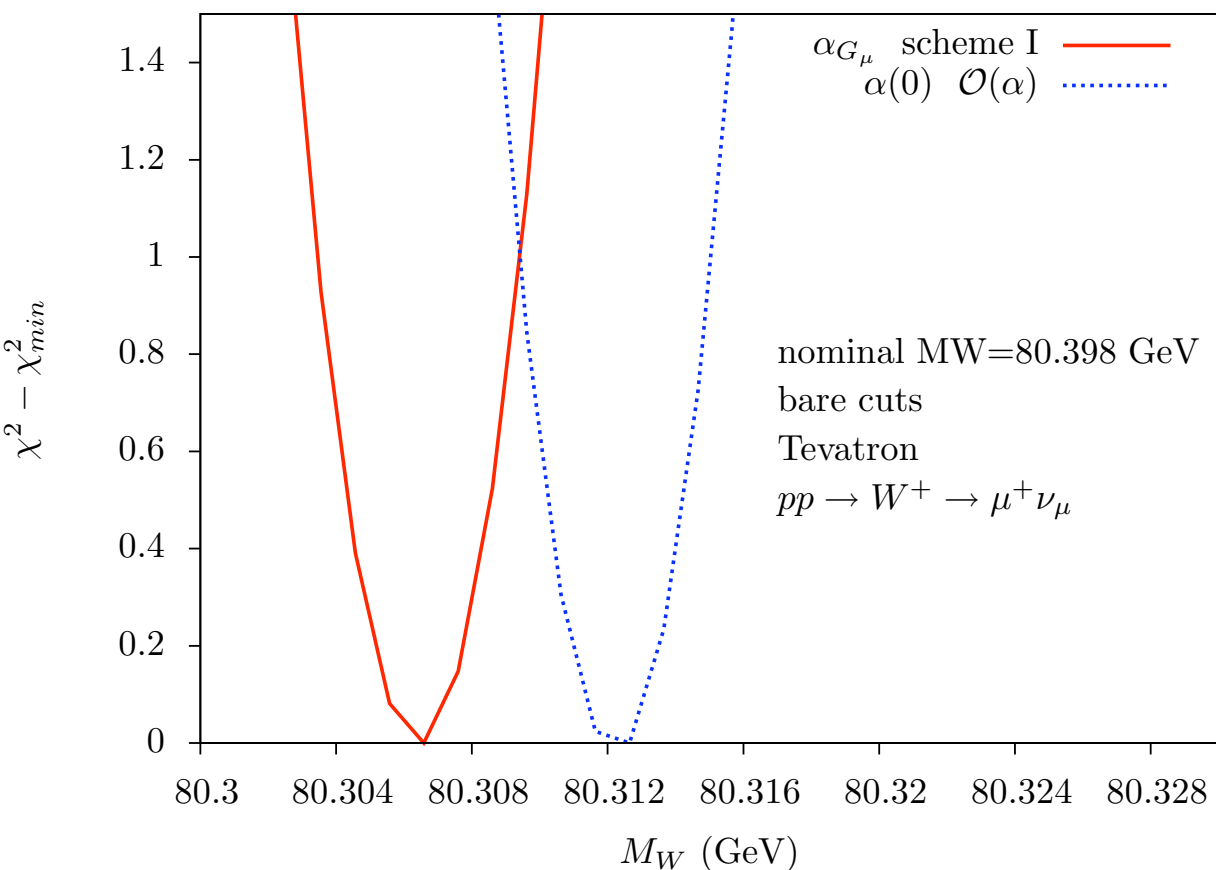
# EW higher orders, Gmu scheme: percentual effect (in unit Born)



The curves obtained with FSR QED Parton Shower are close to the exact 1-loop and to the matched calculation thanks to the input choice

# EW input schemes

Born templates Gmu scheme with 10 billions of events: maximal accuracy 2 MeV



At  $\mathcal{O}(\alpha)$

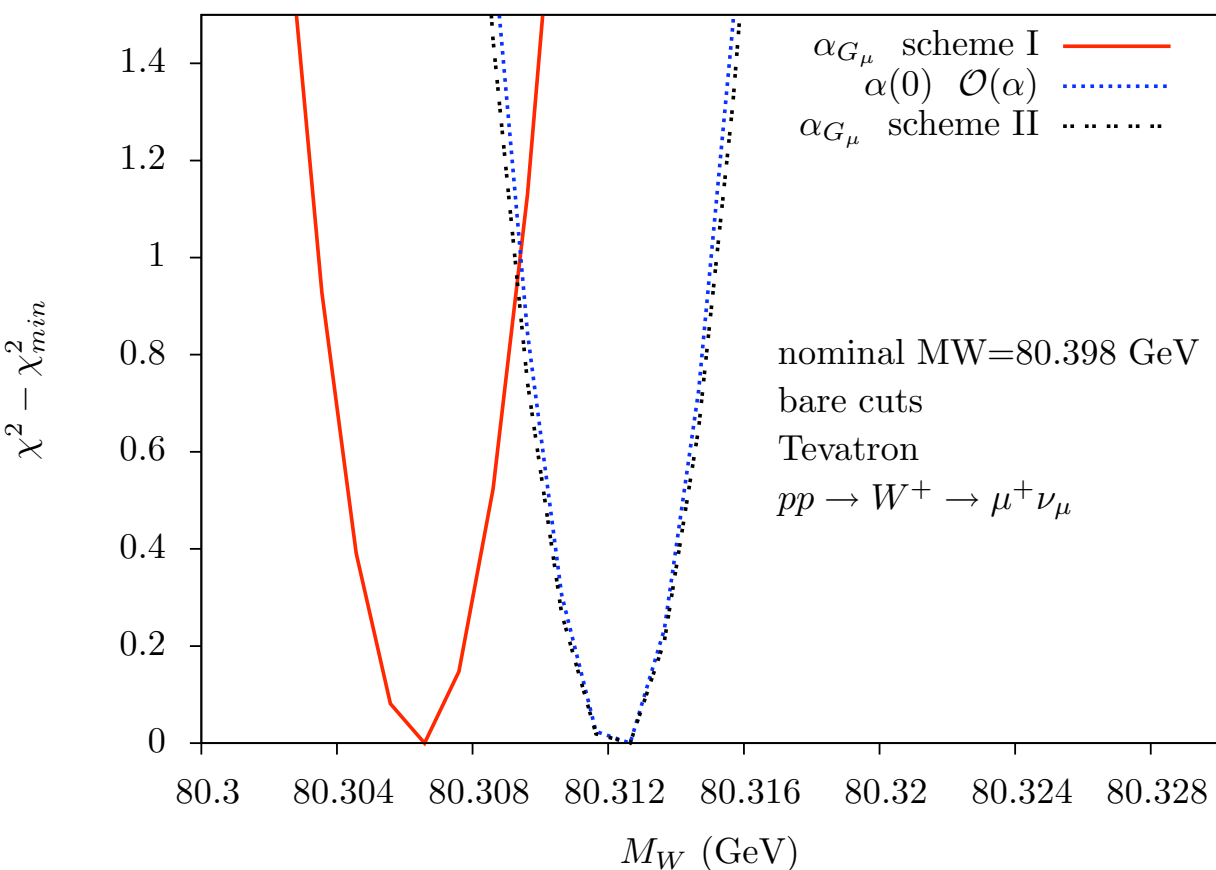
using  $\alpha_0$  or Gmu-I schemes

(different 0- and 1-photon sharing)

yields a change of  $M_W$  of 6 MeV

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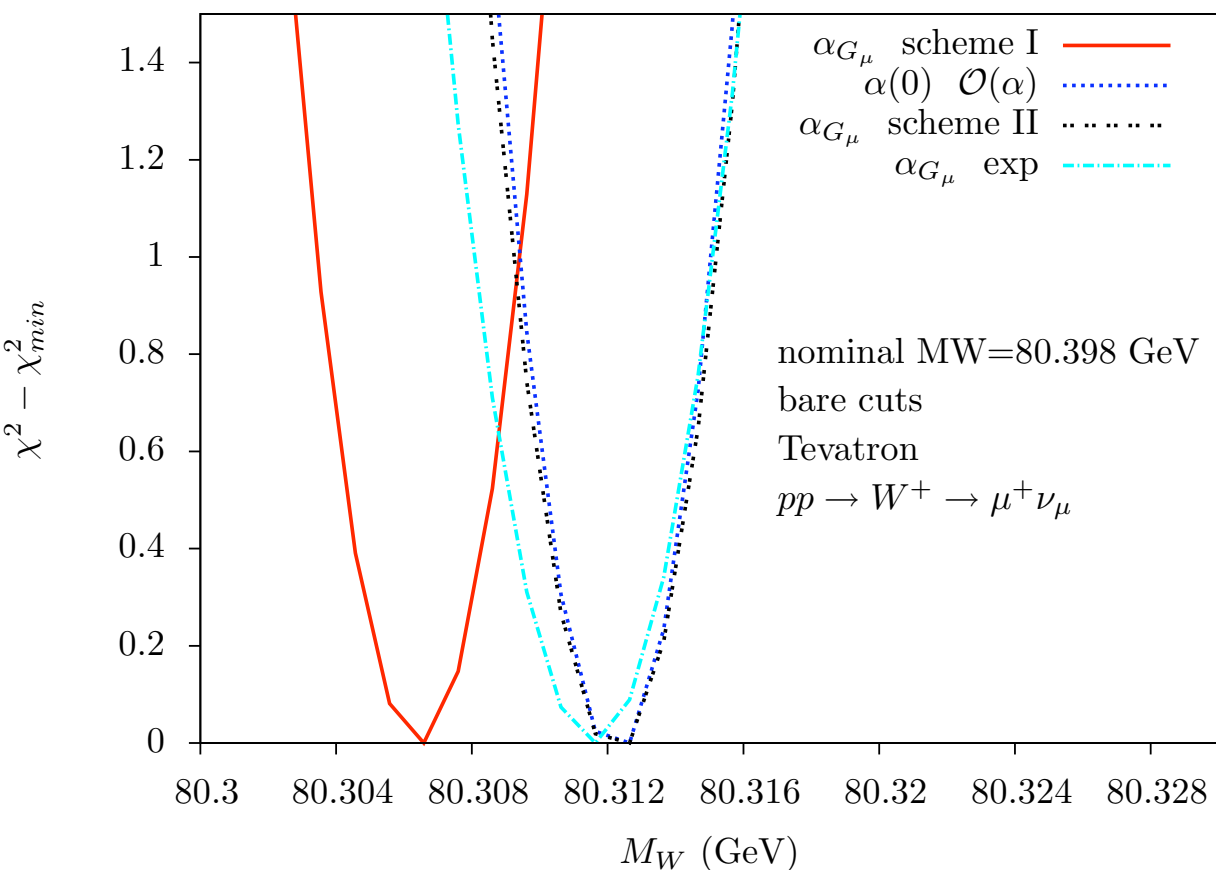
using  $\alpha_0$  or Gmu-II scheme

(same 0- and 1-photon sharing as  $\alpha_0$ )

there is no extra shift in  $M_W$

# EW input schemes

Born templates Gmu scheme with 10 billions of events: maximal accuracy 2 MeV



At  $\mathcal{O}(\alpha)$

using  $\alpha_0$  or Gmu-I schemes  
(different 0- and 1-photon sharing)  
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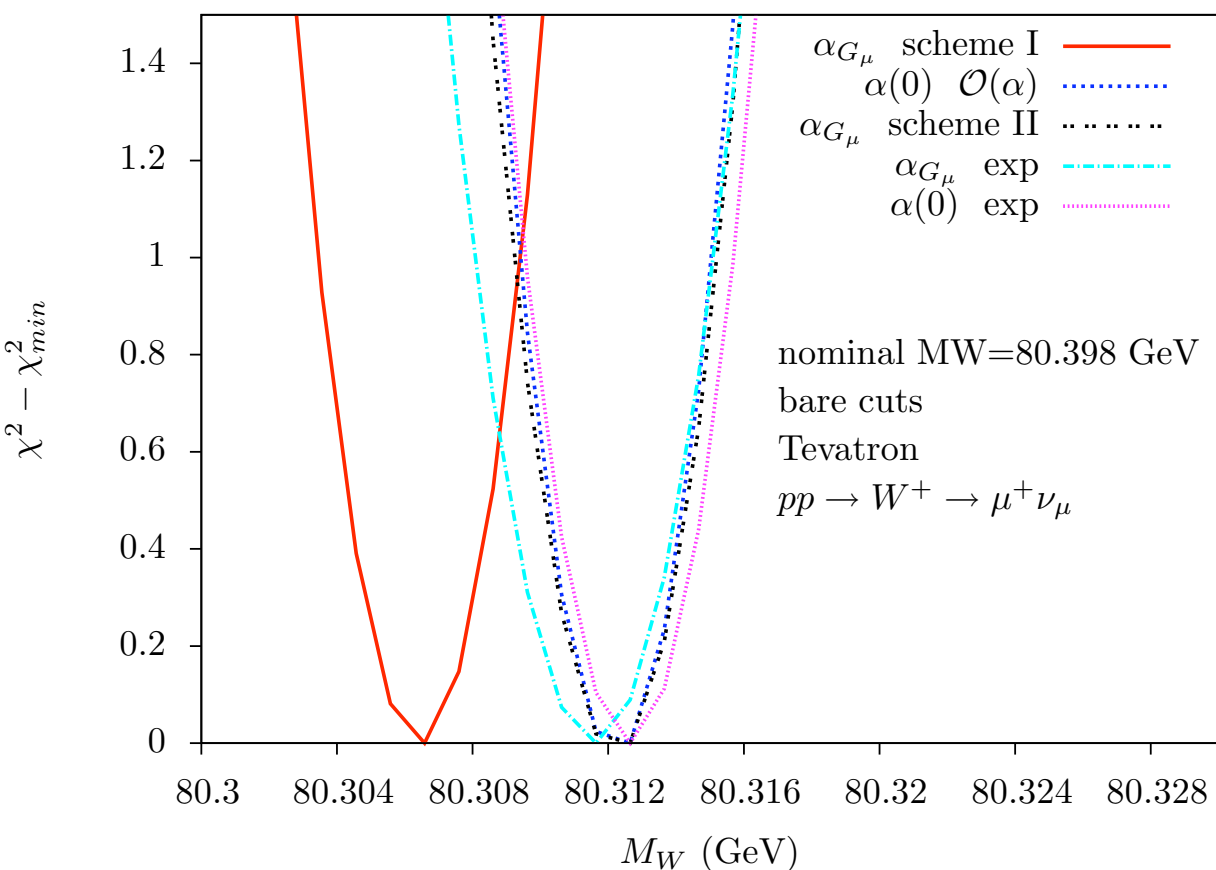
In the Gmu-I scheme

$\mathcal{O}(\alpha)$  and best approximation  
differ by 5 MeV



# EW input schemes

Born templates Gmu scheme with 10 billions of events: maximal accuracy 2 MeV



At  $\mathcal{O}(\alpha)$

using  $\alpha_0$  or Gmu-I schemes  
(different 0- and 1-photon sharing)  
yields a change of  $M_W$  of 6 MeV

At  $\mathcal{O}(\alpha)$

using  $\alpha_0$  or Gmu-II scheme  
(same 0- and 1-photon sharing as  $\alpha_0$ )  
there is no extra shift in  $M_W$

In the Gmu-I scheme

$\mathcal{O}(\alpha)$  and best approximation  
differ by 5 MeV

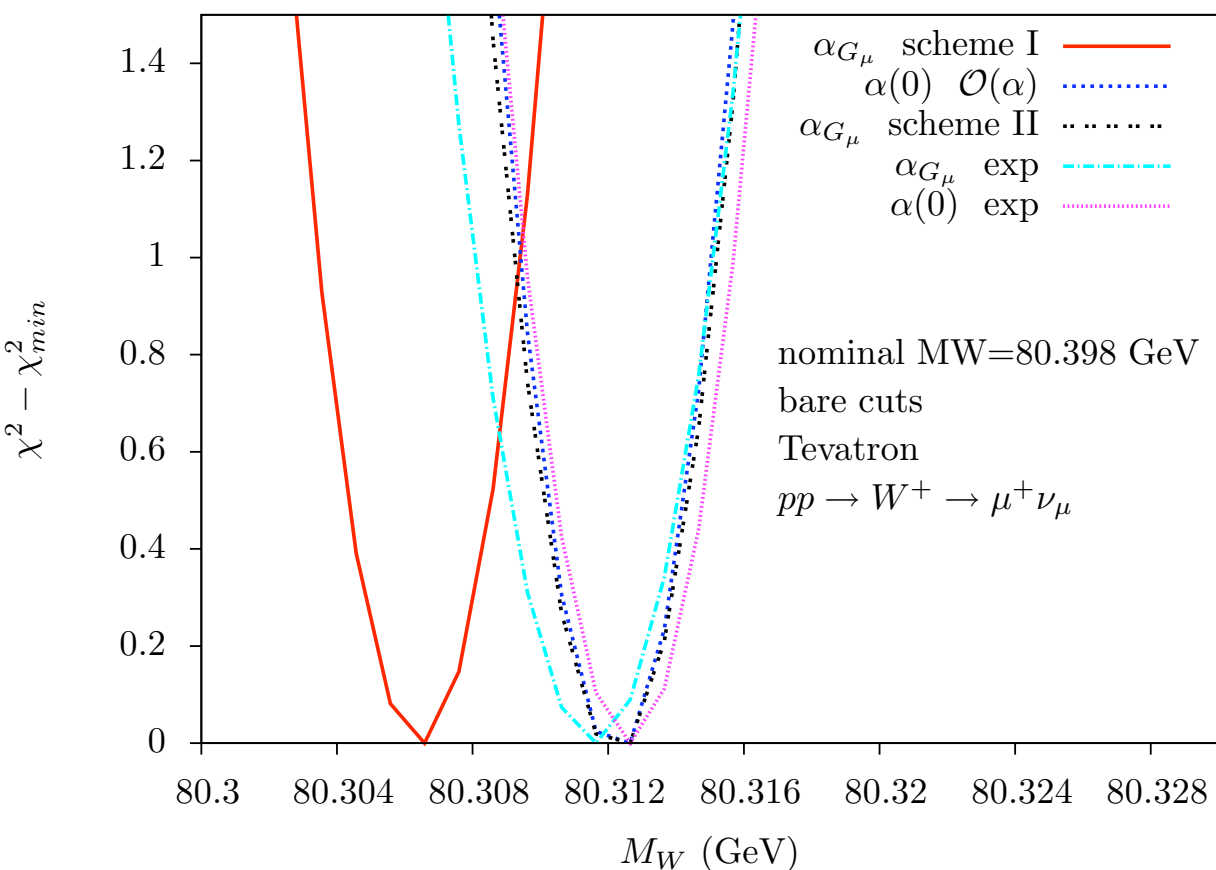
In the best approximation

$\alpha_0$  or Gmu-I schemes  
differ by 2 MeV

(different normalization)

# EW input schemes

Born templates Gmu scheme with 10 billions of events: maximal accuracy 2 MeV



Good stability of the matched formula against scheme changes

Different schemes may yield at most a change of the  $\chi^2$  of the fit

At  $\mathcal{O}(\alpha)$

using  $\alpha_0$  or Gmu-I schemes  
(different 0- and 1-photon sharing)  
yields a change of MW of 6 MeV

At  $\mathcal{O}(\alpha)$

using  $\alpha_0$  or Gmu-II scheme  
(same 0- and 1-photon sharing as  $\alpha_0$ )  
there is no extra shift in MW

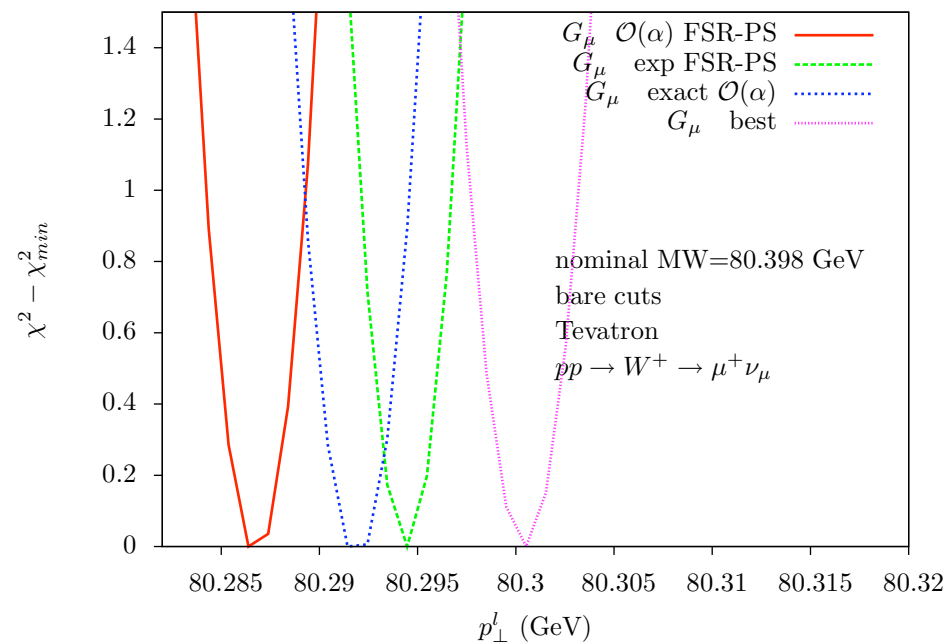
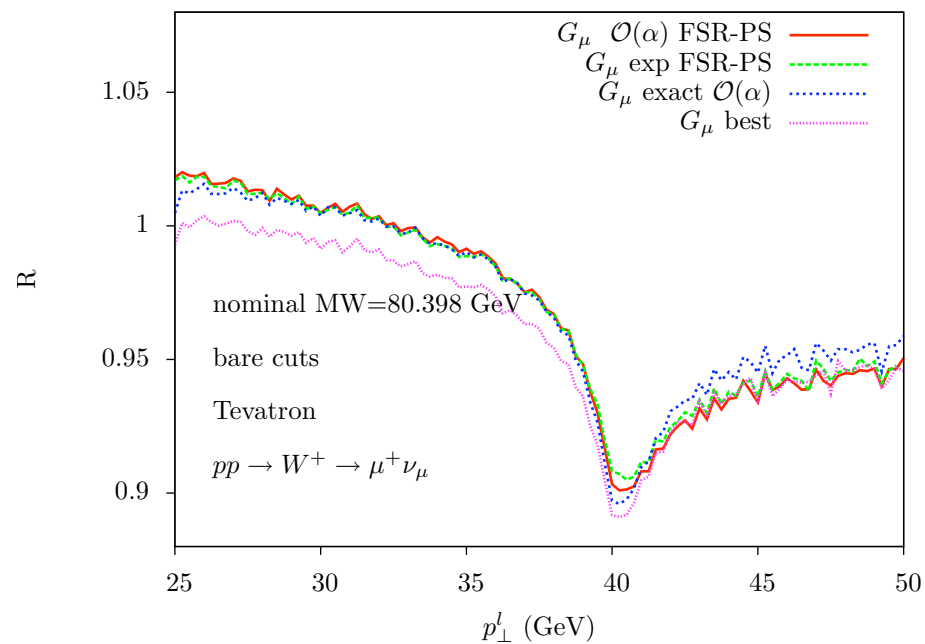
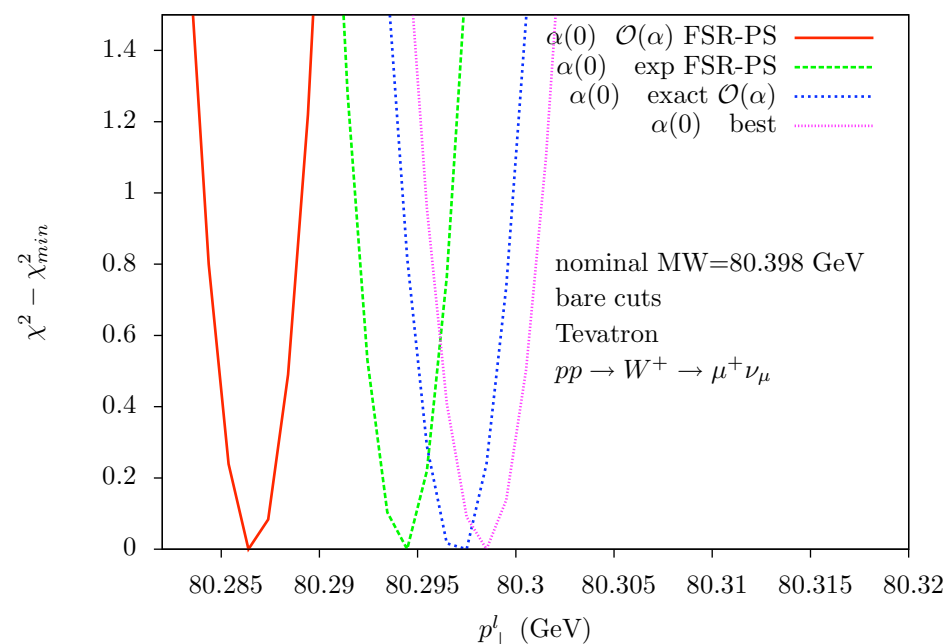
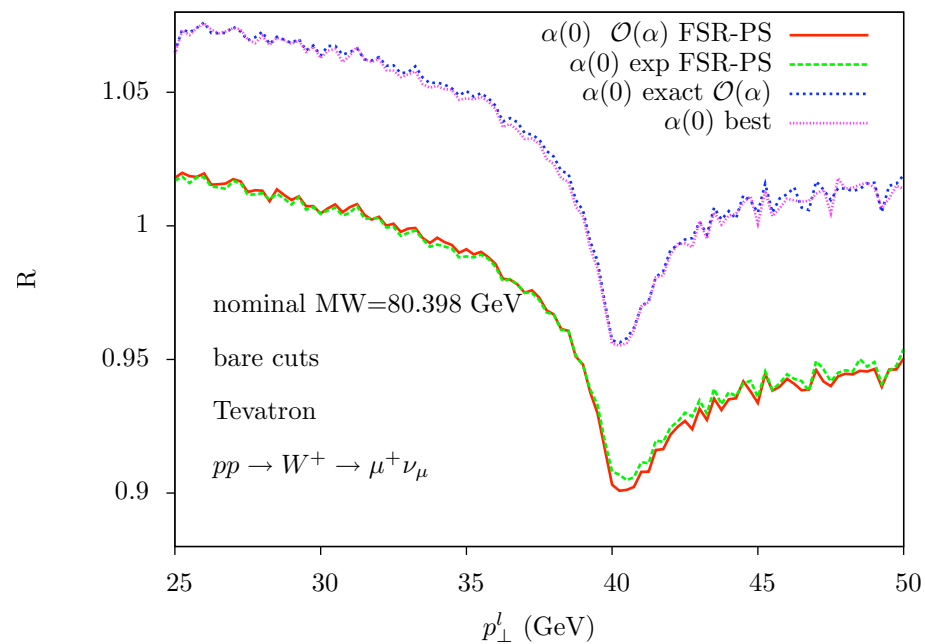
In the Gmu-I scheme

$\mathcal{O}(\alpha)$  and best approximation  
differ by 5 MeV

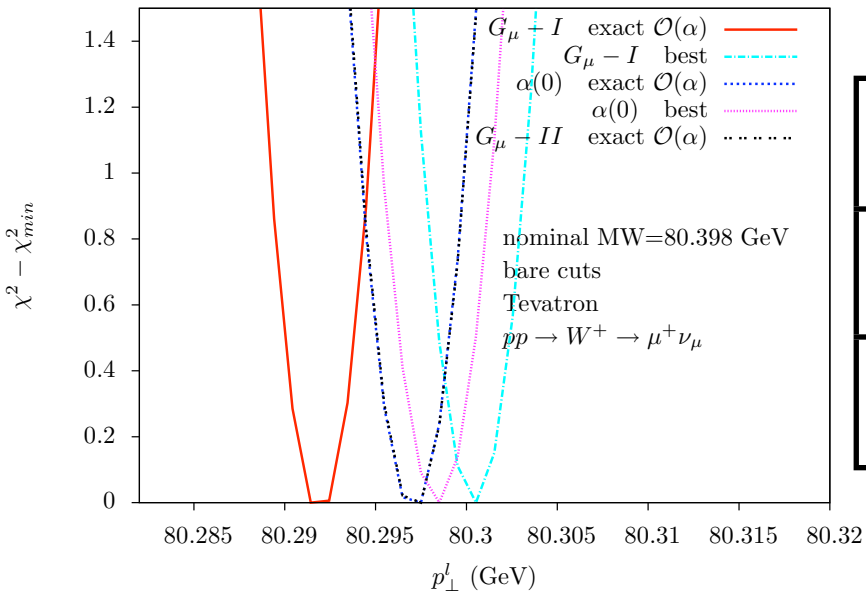
In the best approximation

$\alpha_0$  or Gmu-I schemes  
differ by 2 MeV  
(different normalization)

# EW input schemes: lepton transverse momentum distribution



# EW input schemes: lepton transverse momentum distribution



|                   | truncated<br>$\mathcal{O}(\alpha)$ QED-PS | all orders QED-<br>PS | exact $\mathcal{O}(\alpha)$ | best     |
|-------------------|---|-----------------------|-----------------------------|----------|
| $\alpha_0$ scheme | -112 MeV                                  | -104 MeV              | -101 MeV                    | -100 MeV |
| Gmu<br>scheme     | -112 MeV                                  | -104 MeV              | -107 MeV                    | -98 MeV  |

Good stability of the matched formula against scheme changes:  
the best approximation shows a sensitivity to the scheme choice reduced  
by a factor 3 w.r.t. to the fixed  $\mathcal{O}(\alpha)$  result.

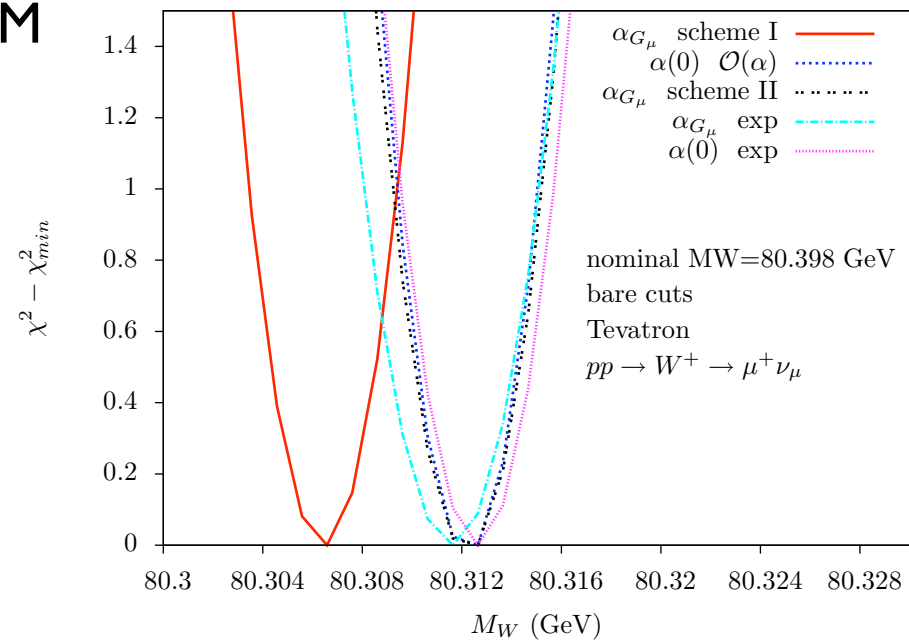
# EW input schemes and MW beyond SM

With the SM templates, MW is measured in the SM

A measurement in the MSSM  
could in principle yield different results

The difference between SM and MSSM  
enters via  $\Delta r$

The input scheme prescription (Gmu-I vs Gmu-II)  
or the fixed order vs matched approximations  
may or may not yield a different final result



# Present uncertainties

CDF uses

Resbos for the QCD simulation

and applies

EW corrections with W/ZGRAD

exact fixed order, no multiple photon

Transverse Mass Fit Uncertainties (MeV)  
(CDF, PRL 99:151801, 2007; Phys. Rev. D 77:112001, 2008)

|                                  | <i>electrons</i> | <i>muons</i> | <i>common</i> |
|----------------------------------|------------------|--------------|---------------|
| W statistics                     | 48               | 54           | 0             |
| Lepton energy scale              | 30               | 17           | 17            |
| Lepton resolution                | 9                | 3            | -3            |
| Recoil energy scale              | 9                | 9            | 9             |
| Recoil energy resolution         | 7                | 7            | 7             |
| Selection bias                   | 3                | 1            | 0             |
| Lepton removal                   | 8                | 5            | 5             |
| Backgrounds                      | 8                | 9            | 0             |
| <sup>s</sup> production dynamics | 3                | 3            | 3             |
| → Parton dist. Functions         | 11               | 11           | 11            |
| QED rad. Corrections             | 11               | 12           | 11            |
| Total systematic                 | 39               | 27           | 26            |
| Total                            | 62               | 60           |               |



## Summary of uncertainties

| Source  | $\sigma(m_W)$ MeV $m_T$ | $\sigma(m_W)$ MeV $p_T^e$ | $\sigma(m_W)$ MeV $E_T$ |
|---|-------------------------|---------------------------|-------------------------|
| <b>Experimental</b>                                 |                         |                           |                         |
| Electron Energy Scale                               | 34                      | 34                        | 34                      |
| Electron Energy Resolution Model                    | 2                       | 2                         | 3                       |
| Electron Energy Nonlinearity                        | 4                       | 6                         | 7                       |
| W and Z Electron energy loss differences (material) | 4                       | 4                         | 4                       |
| Recoil Model  | 6                       | 12                        | 20                      |
| Electron Efficiencies                               | 5                       | 6                         | 5                       |
| Backgrounds   | 2                       | 5                         | 4                       |
| <b>Experimental Total</b>                           | <b>35</b>               | <b>37</b>                 | <b>41</b>               |
| <b>W production and decay model</b>                 |                         |                           |                         |
| PDF   | 9                       | 11                        | 14                      |
| QED   | 7                       | 7                         | 9                       |
| Boson $p_T$   | 2                       | 5                         | 2                       |
| <b>W model Total</b>                                | <b>12</b>               | <b>14</b>                 | <b>17</b>               |
| <b>Total</b>  | <b>37</b>               | <b>40</b>                 | <b>44</b>               |
| <b>statistical</b>                                  | <b>23</b>               | <b>27</b>                 | <b>23</b>               |
| <b>total</b>  | <b>44</b>               | <b>48</b>                 | <b>50</b>               |

systematic uncertainties

D0 uses

Resbos for the QCD simulation

and applies

QED corrections with PHOTOS

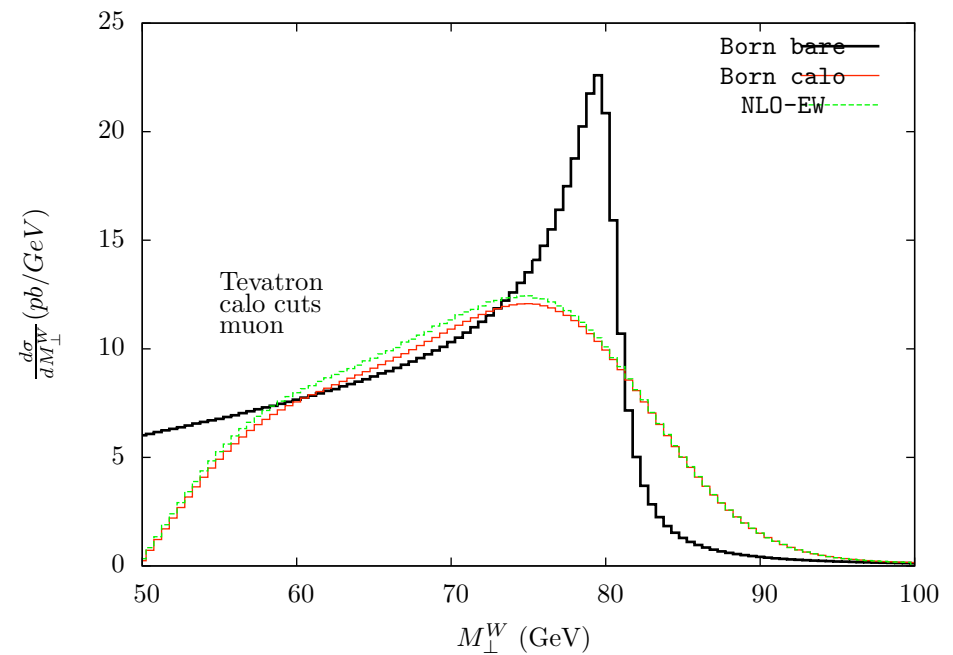
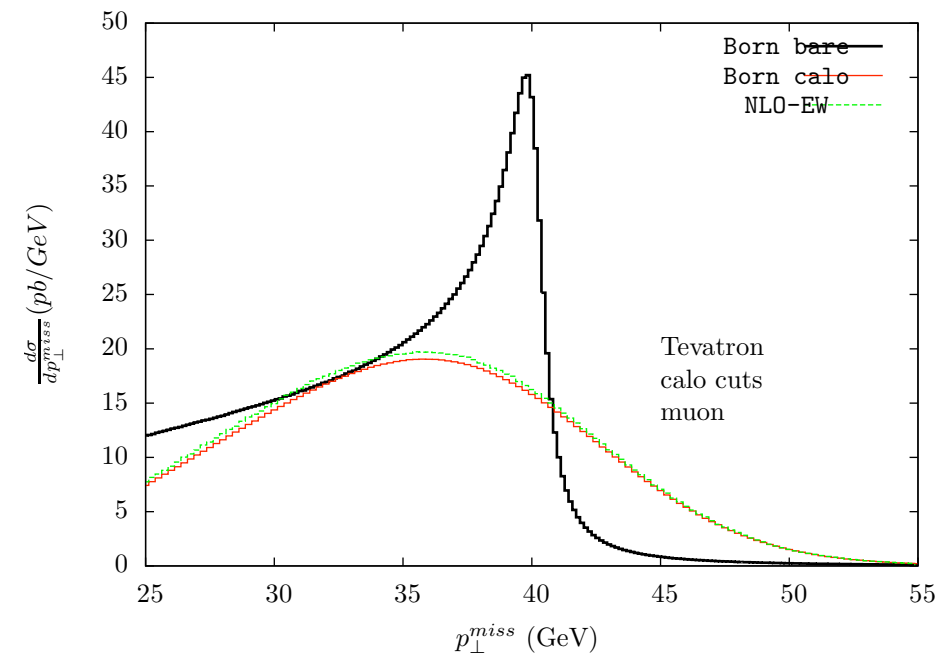
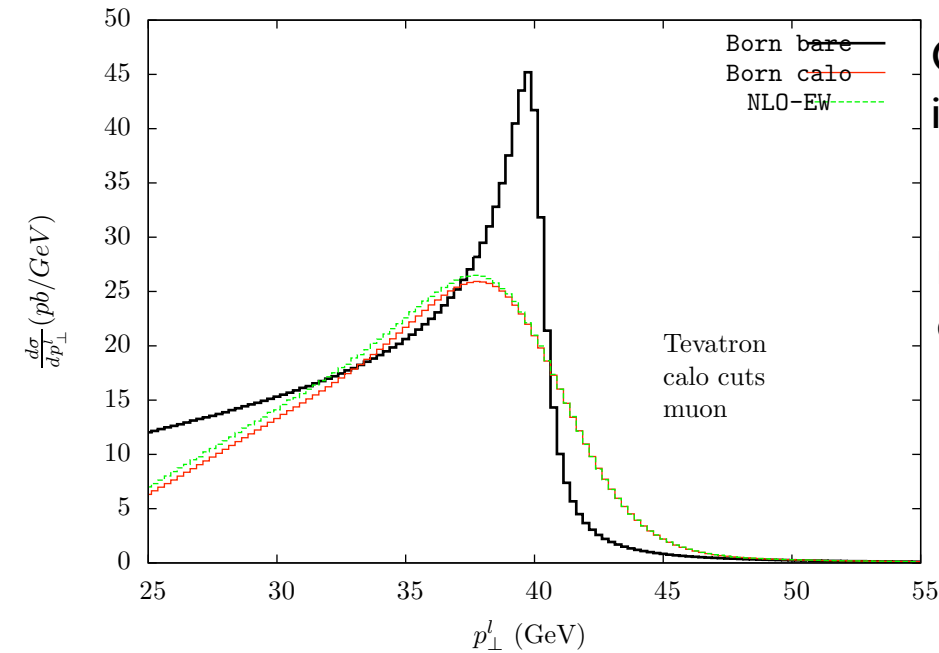
FSR multiple photon

# The effect of smearing the momenta and of photon recombination

Calorimetric energy deposit  
is not pointlike but approximated. by gaussian distribution  
→ smearing of the lepton momenta

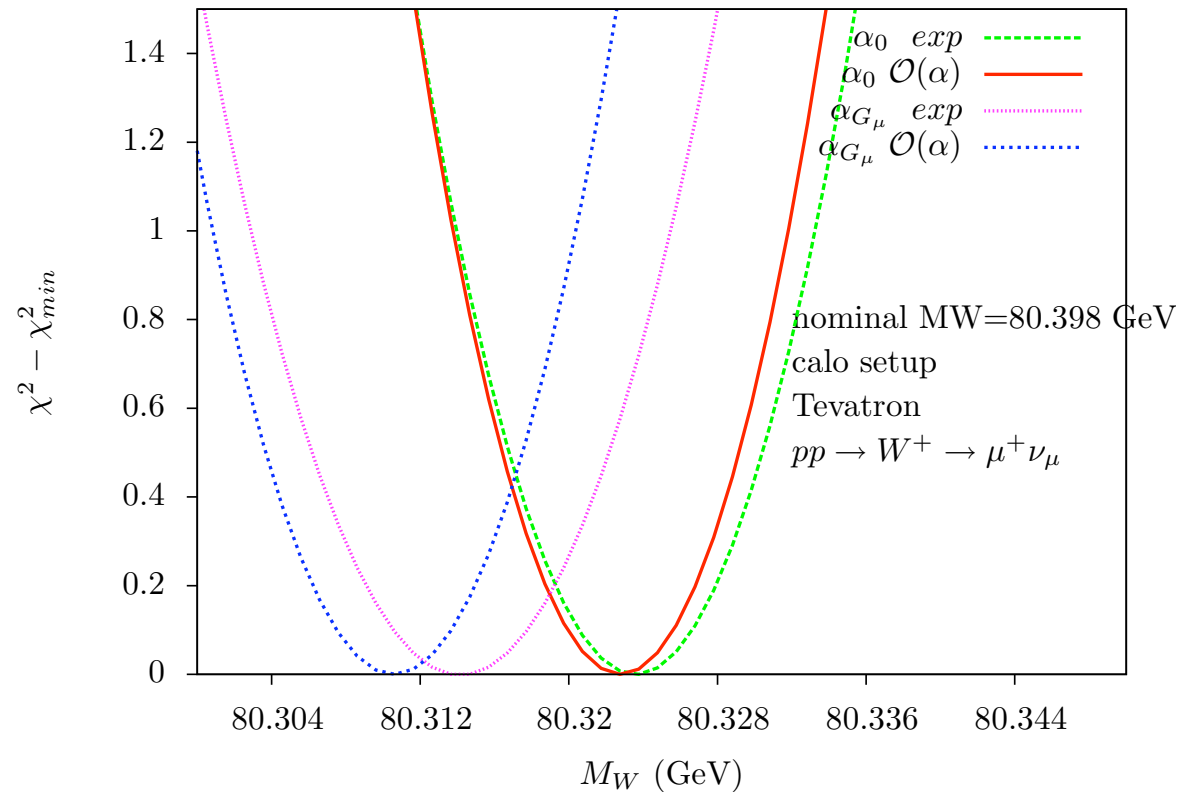
Photons “close” to the emitting lepton are hardly  
disentangled: they are rather merged with the lepton  
need to simulate these events by adding photon and  
lepton momenta to yield an effective lepton  
Effective partial KLN cancellation of FSR collinear logs

How do the effects of higher order corrections survive  
after smearing + recombination?  
Effects measured with smeared Born templates



# EW corrections impact after smearing and recombination

calo Born templates with 1 billions of events: maximal accuracy 4 MeV  
calo setup: smeared lepton momenta (at tree level no recombination)



In the  $\alpha_0$ , best w.r.t. fixed  $O(\alpha)$  results differ by 1 MeV

In the  $G_{\mu-I}$  scheme best w.r.t. fixed  $O(\alpha)$  results differ by 4 MeV



# Conclusions

Final state one-photon emission yields the bulk of the ME shift due to EW corrections

The effect of the inclusion of multiple photon radiation is about 10% of the  $O(\alpha)$  emission and with opposite sign

The effect of the EW, sub-leading  $O(\alpha)$  terms is between 5 and 10% of the leading terms and depends on the chosen EW input scheme

The matched formula by HORACE

- includes the exact  $O(\alpha)$  corrections and the multiple photon radiation
- shows a good stability under EW input scheme changes (shift at the 2 MeV level)

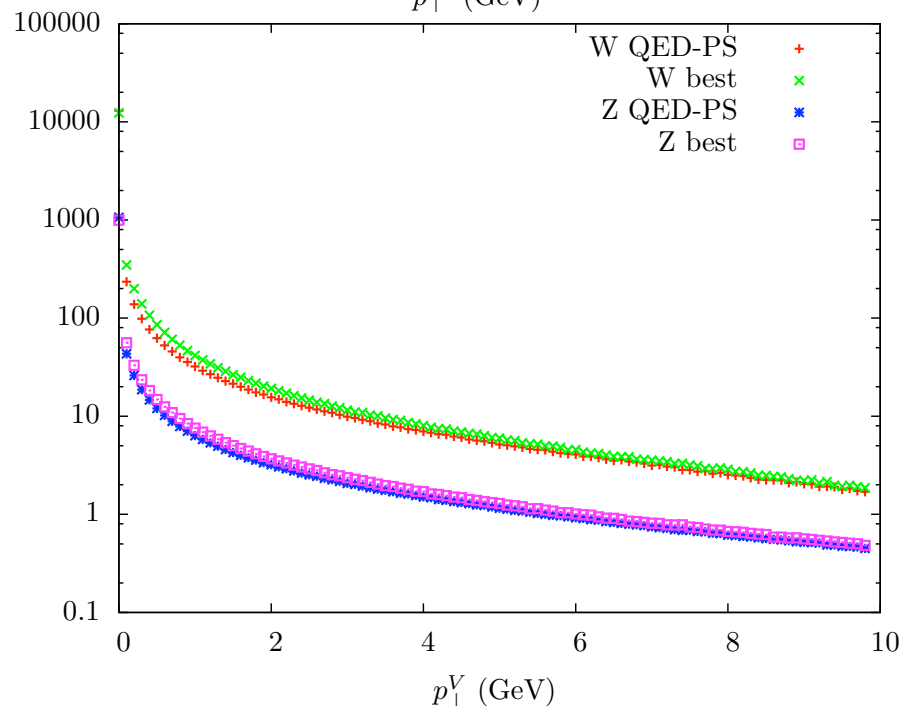
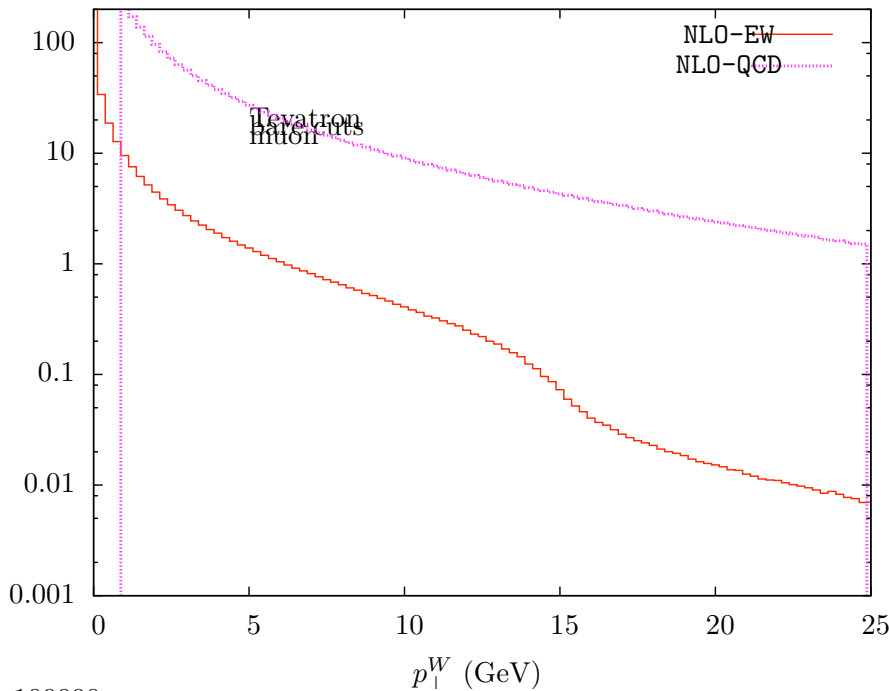
# QED induced $W(Z)$ transverse momentum

The uncertainty on  $pt_W$  directly translates into an uncertainty on the final  $M_W$  value.

Photon radiation yields a tiny gauge boson transverse momentum.

This momentum is different in the CC and NC channels because of the different flavor structure.

The “non-final state” component differs in the 2 cases by  $54 (Z) - 33 (W) = 21 \text{ MeV}$



|                                 |          |       |     |
|---------------------------------|----------|-------|-----|
| $\langle p_{\perp}^V \rangle =$ | Z FSR-PS | 0.409 | GeV |
|                                 | Z best   | 0.463 | GeV |
|                                 | W FSR-PS | 0.174 | GeV |
|                                 | W best   | 0.207 | GeV |

The fit of the non perturbative QCD parameters is done on the Z transverse momentum and it is necessary to properly remove the EW corrections to the NC channel

In the simulation of the CC channel the relevant EW corrections are then applied

# Validation of the template-fitting procedure

In this template-fitting procedure,

the reduced  $\chi^2$  is never close to one because the distributions are “by construction” different

Fit pseudo-data computed in Born approximation reduced  $\chi^2 \sim 1$

The fit should **exactly** find the nominal value  $M_W^0$  used to generate the Born pseudo-data

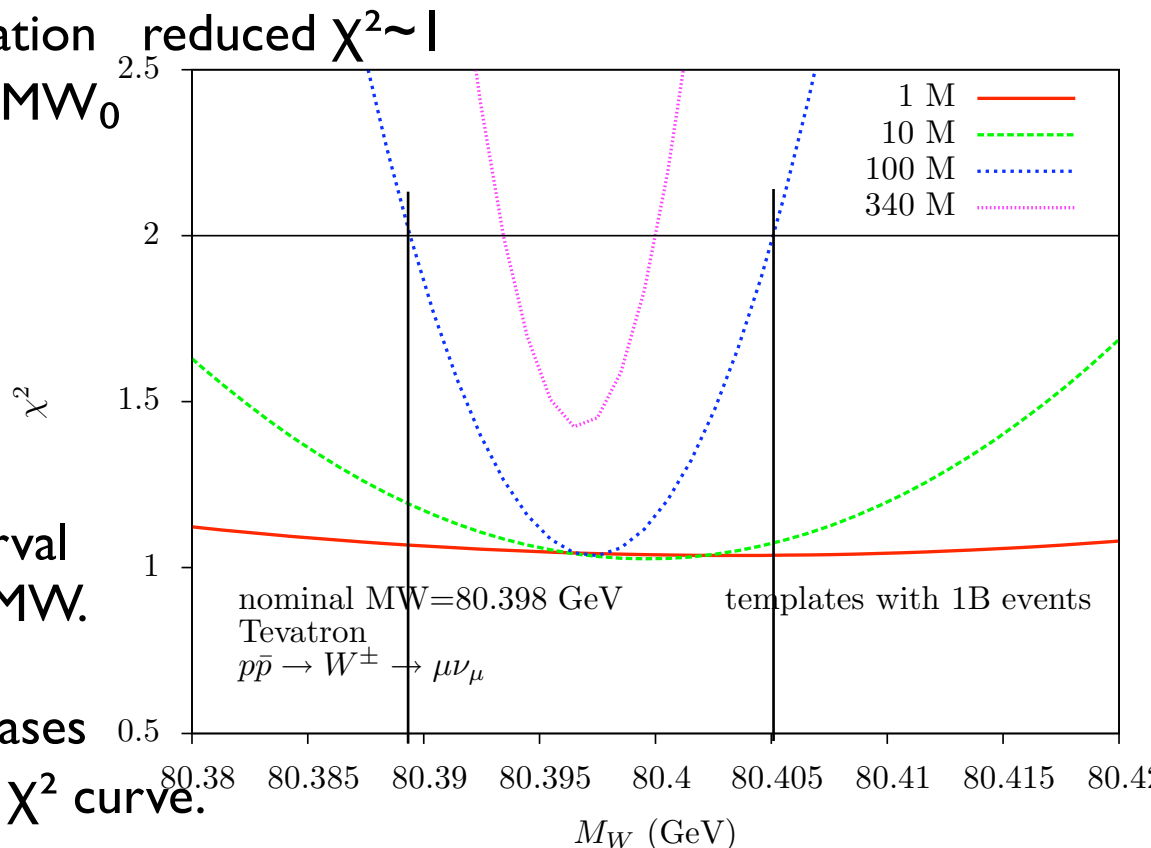
The accuracy of the fit depends on the error associated to each bin of the pseudo-data

In the case of Born pseudo-data, the  $\Delta\chi^2 = 1$   $M_W$  points fix the 68% C.L. interval associated to the estimate of the preferred  $M_W$ .

A larger number of pseudo-data events increases the accuracy of the prediction, shrinking the  $\chi^2$  curve.

The templates are not smooth functions, but are generated with a Montecarlo  
They also suffer of statistical fluctuations.

We can not arbitrarily increase the number of pseudo-data events, because we are limited by the number of events used to generate the templates



# EW results and tools

$\mathcal{O}(\alpha_S^2) \approx \mathcal{O}(\alpha_{em})$   Need to worry about EW corrections

## W production

|                             |  |                                |
|-----------------------------|--|--------------------------------|
| Pole approximation          | D.Wackeroth and W. Hollik, PRD 55 (1997) 6788<br>U.Baur et al., PRD 59 (1999) 013002   |                                |
| Exact $\mathcal{O}(\alpha)$ | V.A. Zykunov et al., EPJC 3 (2001) 9<br>S. Dittmaier and M. Krämer, PRD 65 (2002) 073007<br>U. Baur and D.Wackeroth, PRD 70 (2004) 073015<br>A.Arbusov et al., EPJC 46 (2006) 407<br>C.M.Carloni Calame et al., JHEP 0612:016 (2006) | DK<br>WGRAD2<br>SANC<br>HORACE |
| Photon-induced processes    | S. Dittmaier and M. Krämer, Physics at TeV colliders 2005<br>A. B.Arbusov and R.R.Sadykov, arXiv:0707.0423   |                                |
| Multiple-photon radiation   | C.M.Carloni Calame et al., PRD 69 (2004) 037301, JHEP 0612:016 (2006)<br>S.Jadach and W.Placzek, EPJC 29 (2003) 325<br>S.Brensing, S.Dittmaier, M. Krämer and M.M.Weber, arXiv:0708.4123   | HORACE<br>WINHAC<br>DK         |

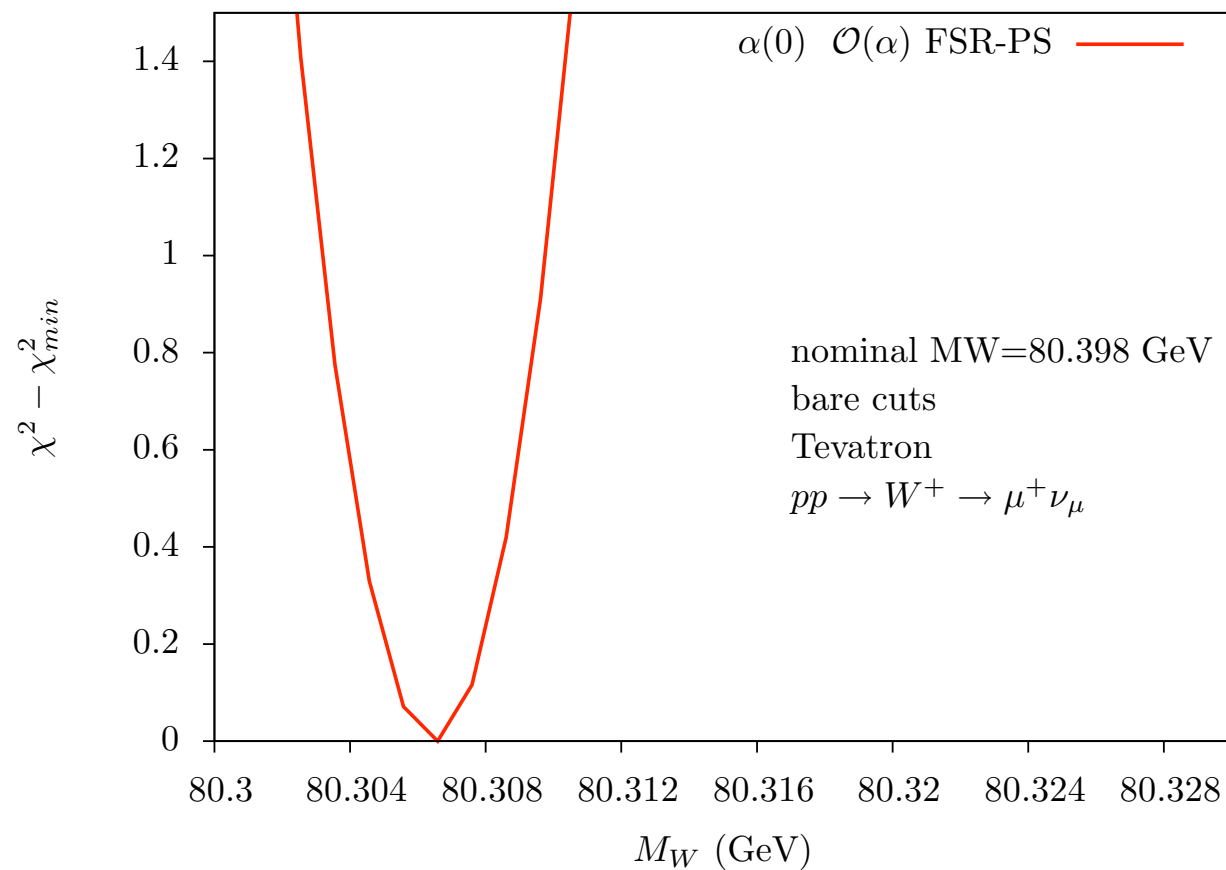
## Z production

|                             |  |                  |
|-----------------------------|--|------------------|
| only QED                    | U.Baur et al., PRD 57 (1998) 199   |                  |
| Exact $\mathcal{O}(\alpha)$ | U.Baur et al., PRD 65 (2002) 033007<br>V.A. Zykunov et al., PRD75 (2007) 073019<br>C.M.Carloni Calame et al., JHEP 0710:109 (2007) | ZGRAD2<br>HORACE |
| Multiple-photon radiation   | C.M.Carloni Calame et al., JHEP 0505:019 (2005)<br>JHEP 0710:109 (2007)  | HORACE           |

# EW higher orders in the $\alpha_0$ scheme

Born templates  $\alpha_0$  scheme with 10 billions of events: maximal accuracy 2 MeV

The FSR QED Parton Shower  
truncated at  $\mathcal{O}(\alpha)$   
yields a change of MW of -92 MeV

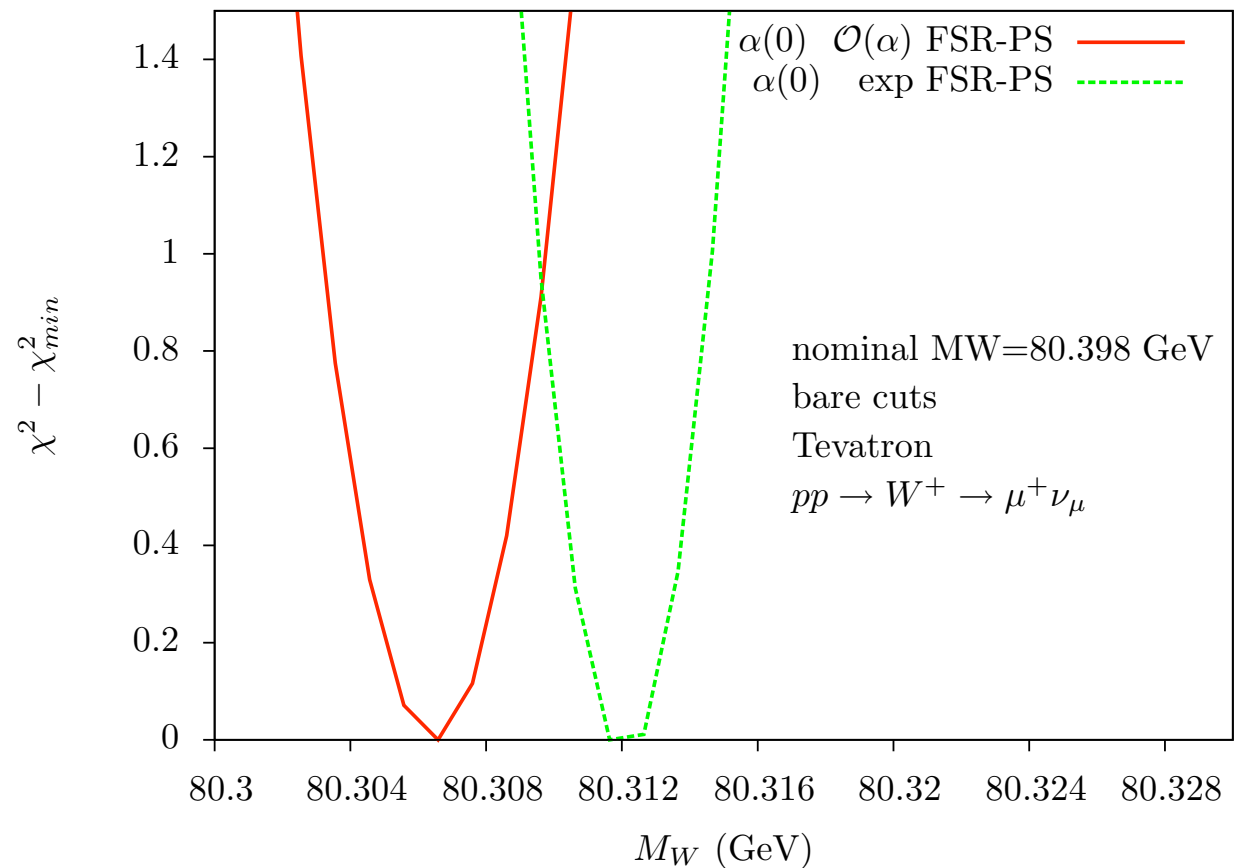


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Born templates  $\alpha_0$  scheme with 10 billions of events: maximal accuracy 2 MeV

The FSR QED Parton Shower truncated at  $\mathcal{O}(\alpha)$  yields a change of MW of -92 MeV

The FSR QED Parton Shower to all orders yields an additional shift of +6 MeV



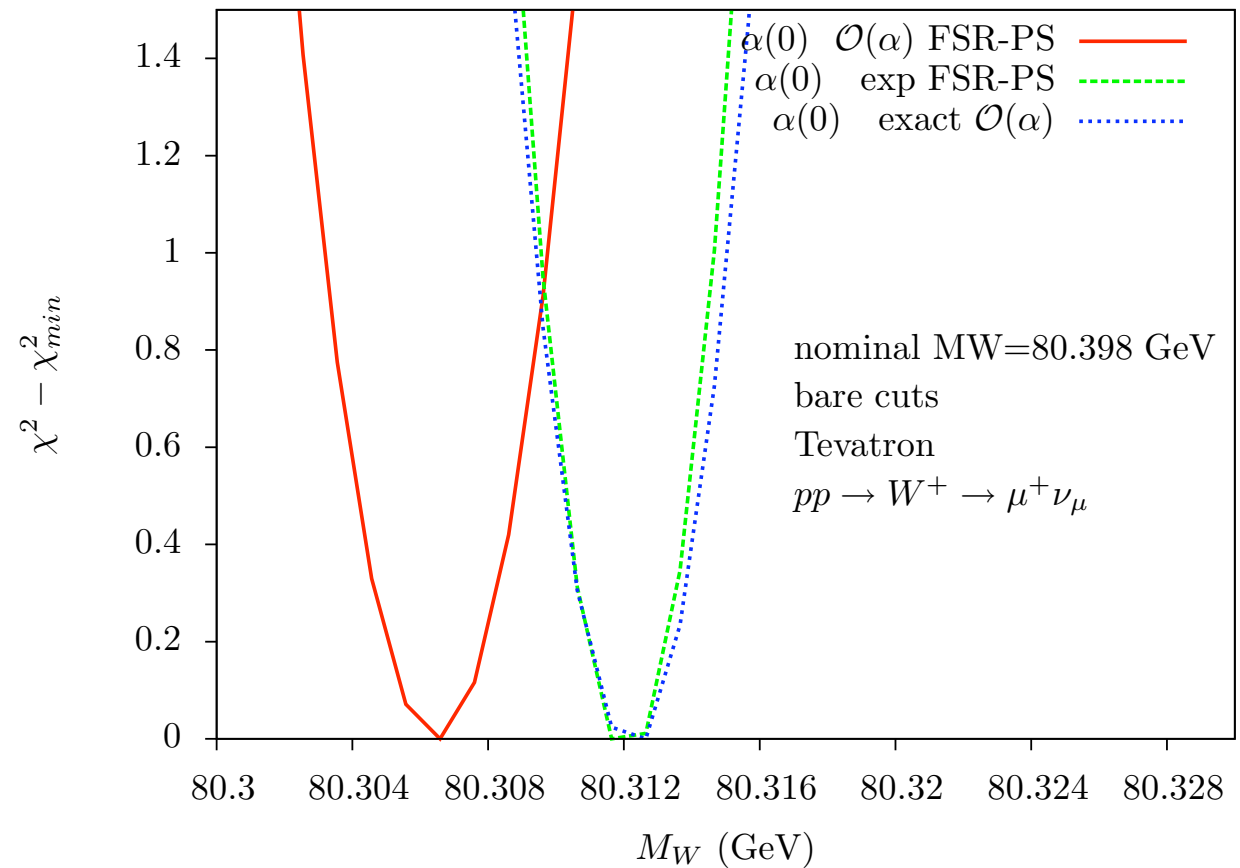
# EW higher orders in the $\alpha_0$ scheme

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The exact matrix element at  $\mathcal{O}(\alpha)$  and  $\mathcal{O}(\alpha)$  FSR QED PS prediction differ by +6 MeV (subleading EW)



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The exact matrix element at  $\mathcal{O}(\alpha)$  and  $\mathcal{O}(\alpha)$  FSR QED PS prediction differ by +6 MeV (subleading EW)

The best matched results  $\mathcal{O}(\alpha)$  + full QED Parton Shower yields no shift (0 MeV) w.r.t. the fixed order exact  $\mathcal{O}(\alpha)$  (which is based on a different formula)  
This results is true in the  $\alpha_0$  scheme

