

# Starlings in flight

*understanding patterns of animal group movements  
from the complex system perspective*

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*European STREP project **STARFLAG***

*Pavia, November 2005*

## STARLING FLOCKS

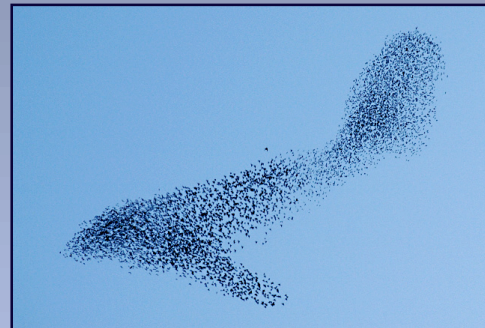
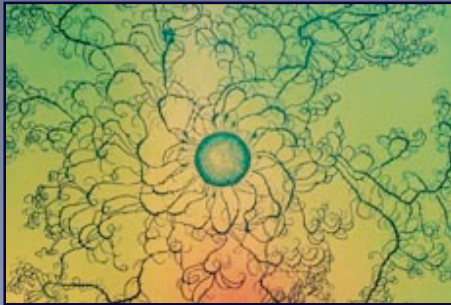


*Termini railway station, Rome  
Evening roosting time, November 2004*



Collective phenomena often occur in biological systems

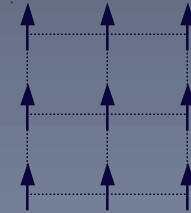
*Bacteria colonies , blood cells, insects swarms, fish schools, birds flocks, quadrupets herds*



What are the rules governing coordination and collective motion ?

Collective phenomena have been widely studied in physics

- *Cooperative behaviour in phase transitions and ordering*
- *Local interactions can generate long range order*
- *Universality, renormalization → the details are not important*
- *Efficient simple models*



### The Physics Paradigm



the microscopic mechanisms determining flocking pattern formation and coordinated collective motion are local and simple and do not depend dramatically on the complex nature of the individuals

*Hypothesis !*

*SIMPLE MODELS*

# Minimal Models of Flocking

*Each individual bird determines its direction of motion on each time step by averaging the direction of its neighbours (allelomimesis) with some noise*

## Self-Propelled Particles

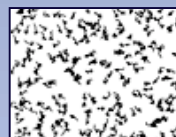
*Reynolds, Comput. Graph., 87  
Vicsek et al., PRL 95*

$$\theta_i(t+1) = \arg \left[ \sum_{j \sim i} \vec{v}_j(t) \right] + \eta_i(t)$$

↓ direction
↓ velocity
↓ noise

- Nonequilibrium analog of the ferromagnetic XY model (in 2D) *Rotational Symmetry*
- Onset of collective motion for small noise, even in 2D (*Mermin-Wagner does NOT hold*)

$$\phi = \frac{1}{Nv} \left| \sum_i \vec{v}_i(t) \right|$$



$$|\eta|=2$$

$$\phi=0$$



$$|\eta|=0.1$$

$$\phi>0$$

- Navier-Stokes like equations for the coarse-grained velocity *Toner & Tu, PRL 1995*

*Convective relevant  
non-linear terms*



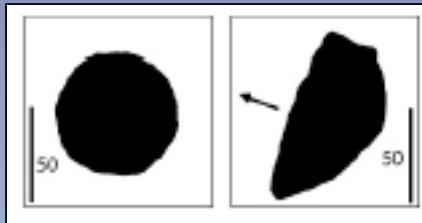
*Non trivial RG fixed point  
Exact exponents in D=2  
Effective long-range interactions*

## SPP with cohesion

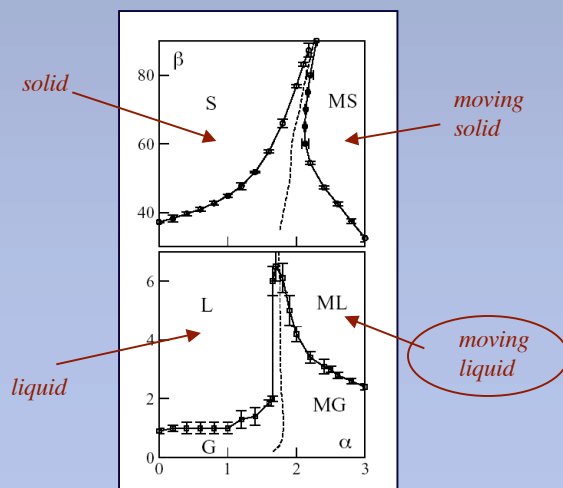
Gregoire, Chate & Tu, PRL 2001  
 Gregoire & Chate, PRL 2004  
 Gregoire, Chate & Tu, PRE 2004

$$\theta_i(t+1) = \left[ \alpha \sum_{i \sim j} \vec{v}_i(t) + \beta \sum_{i \sim j} f_{ij} \right] + \eta_i(t)$$

↓  
 Hard-core repulsion +  
 Short-range attraction ( $r_0$ )



- Non trivial infinite space limit  
*cohesive moving flocks in infinite space*



- Complex phase diagram

$$\phi = \frac{1}{Nv} \left| \sum_i \vec{v}_i(t) \right|$$

Moving/Non moving

$$n_{clust} \quad \Delta_{i \sim j}^{diff}$$

Cohesive/Sparse  
 Gas - Liquid - Solid

- Discontinuous first order transitions



# Experiments

Stereoscopic 3D reconstruction of

- Flock shape and movement
- Individual birds positions
- Individual birds trajectories

## *Stereoscopic Photography*



2 D images



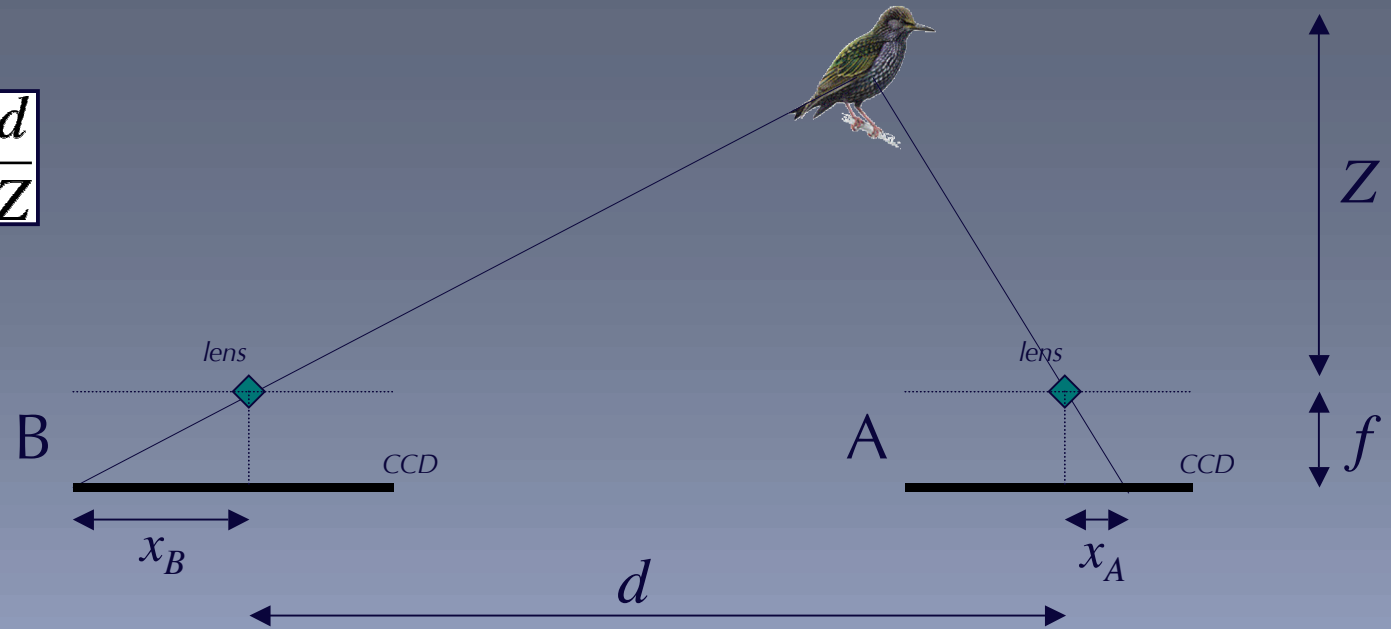
3D coordinates

## *Stereometry*

- image elaboration
- birds recognition
- stereoscopic matching
- epipolar post-calibration

$$s = x_B - x_A = f \frac{d}{Z}$$

*Stereoscopic shift*



- the larger the distance, the better the resolution

*neighbouring birds*

$$\delta s = f \frac{d}{Z^2} \delta Z$$

$$\left. \begin{array}{l} f = 4000 \\ Z = 200 \text{ m} \\ \delta Z = 0.5 \text{ m} \\ \delta s = 1 \end{array} \right\} \Rightarrow d = 20 \text{ m}$$

- misalignments strongly affect absolute distances

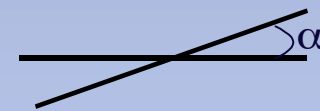
$$\frac{\delta Z}{Z} = \alpha \frac{Z}{d}$$

$$\alpha = 0.001 \text{ rad}$$

$$\delta Z/Z = 2.0 / 200$$

$$\alpha = 0.0003 \text{ rad}$$

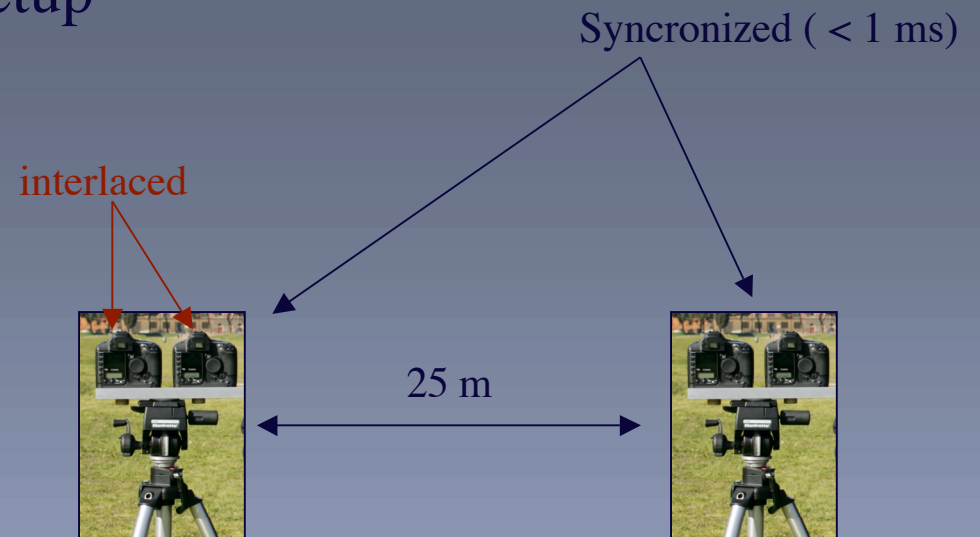
$$\delta Z/Z = 0.5 / 200$$



# The setup

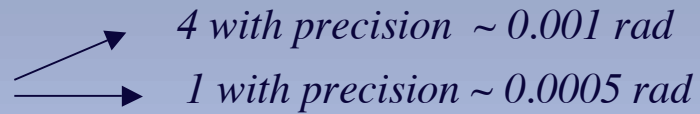


Palazzo Massimo, Rome



- Alignement

*There are 5 external angles to be fixed*



- Calibration

*There are the internal parameters to be calibrated (or postcalibrated)*

- Temporization

5fps @ 16m/s : *birds travel 3.2 m between two consecutive shots*

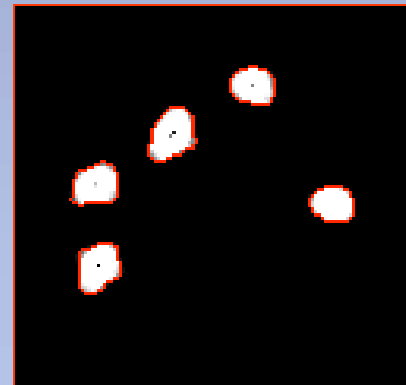
2 interlaced cameras  $\implies$  10 fps    1.6 m

# Matching and 3D reconstruction



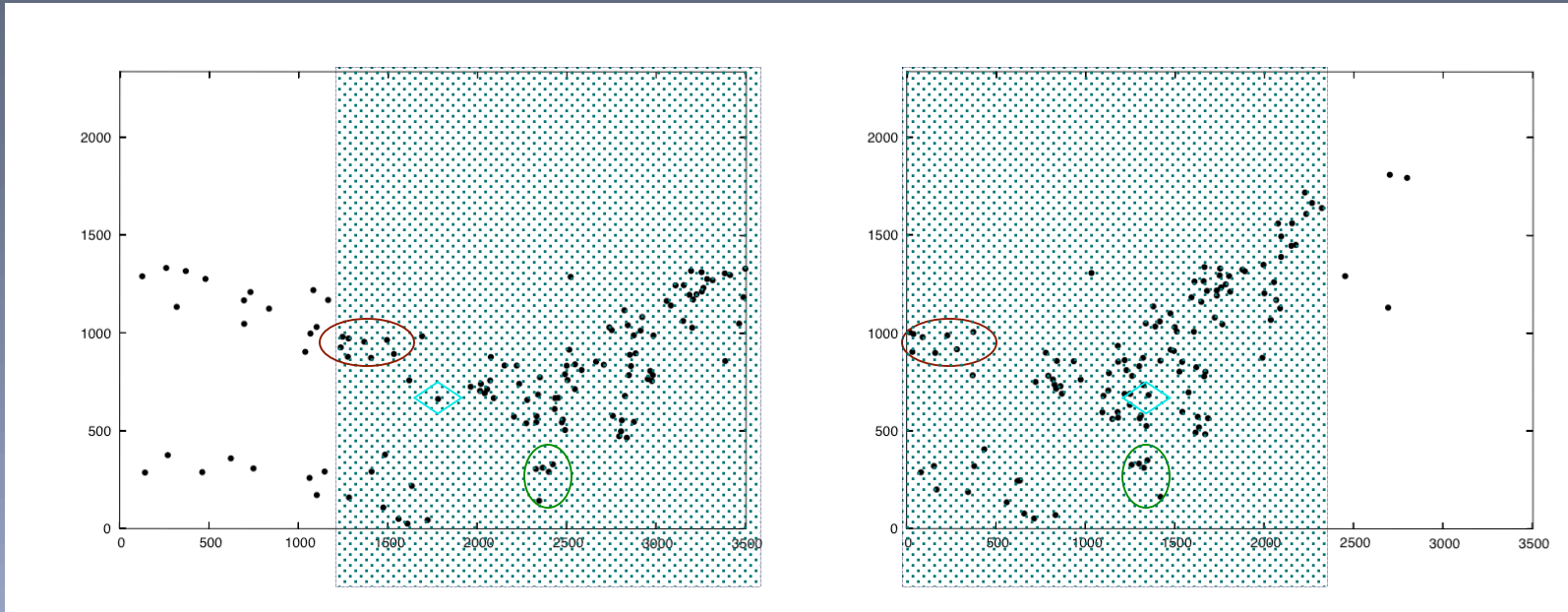
- Bird recognition

Contrast filters, segmentation algorithms





• Matching



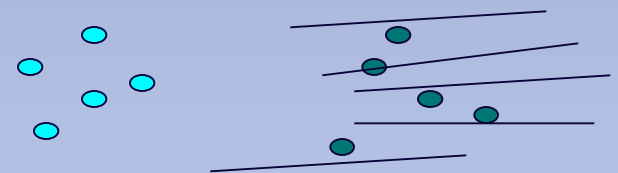
1) Pattern recognition algorithm  $\longrightarrow$  Zero-matching (partial)  $M_0$

2) Epipolar geometry

$$r_B^T F r_A = 0$$

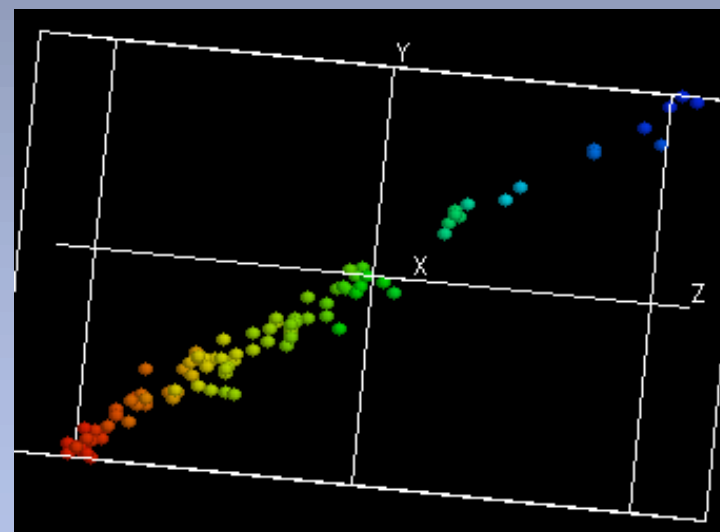
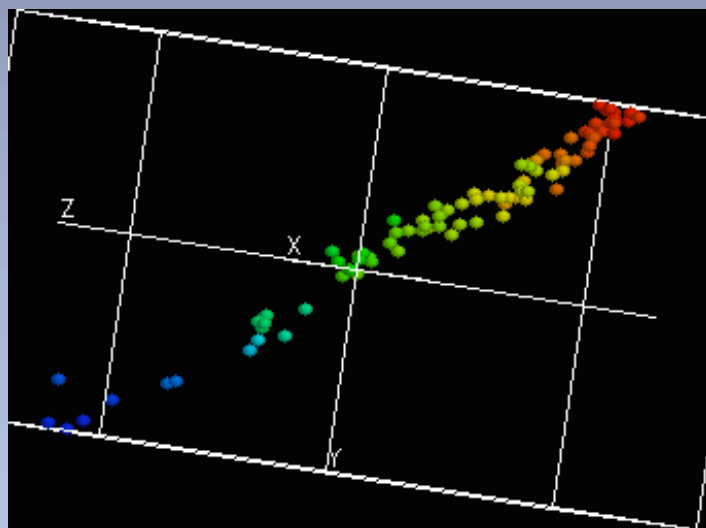
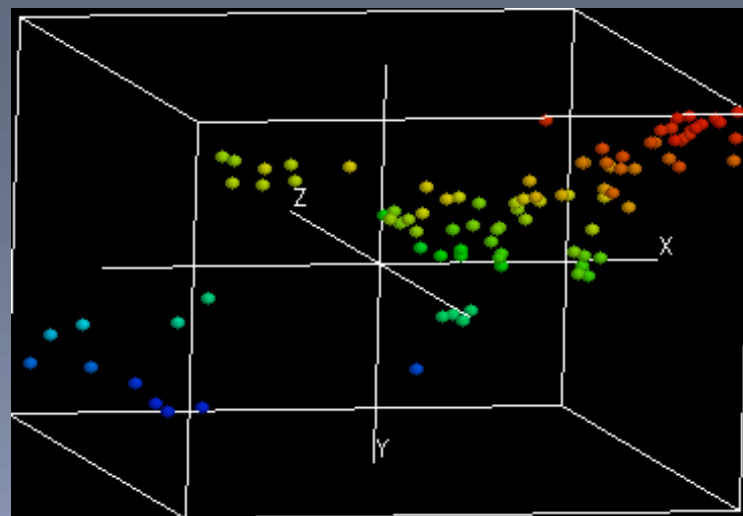
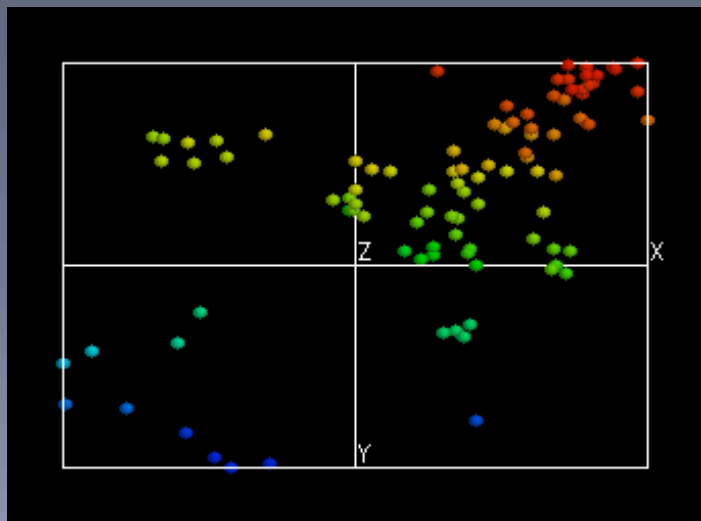
$F =$  *fundamental matrix*

*depends on the angles !  
affected by JPEG Noise*



3) K-assignment

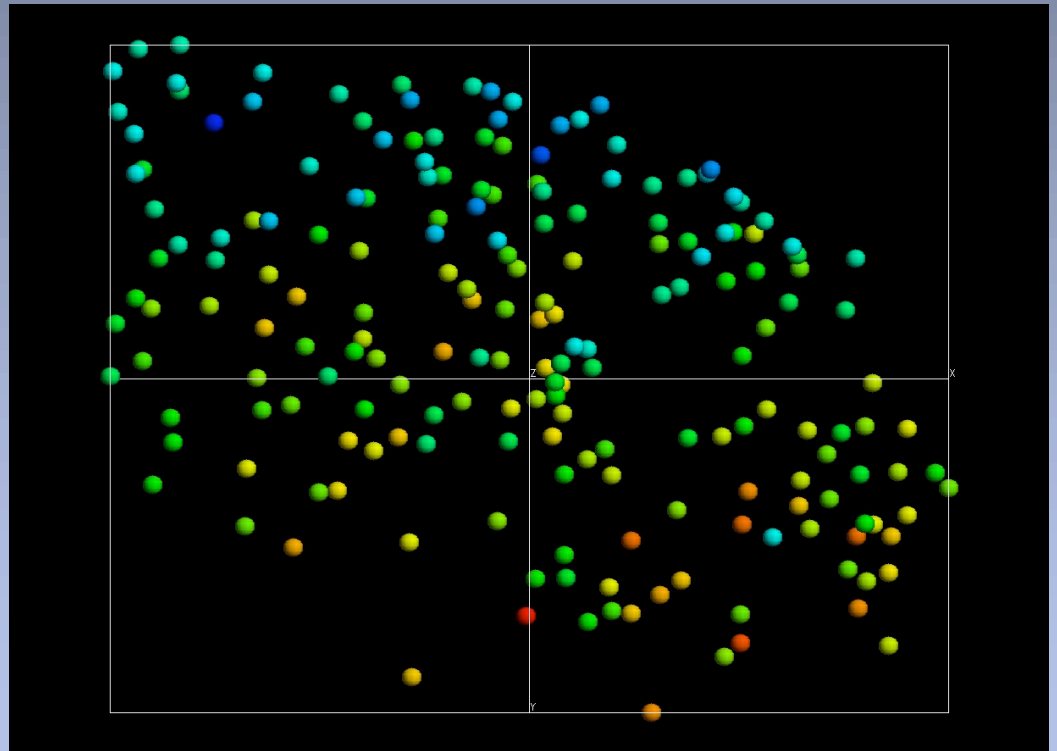
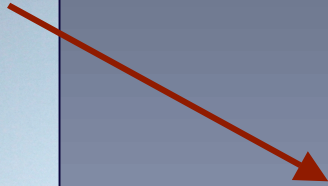
*Matching between different set of points with measure  $F$*

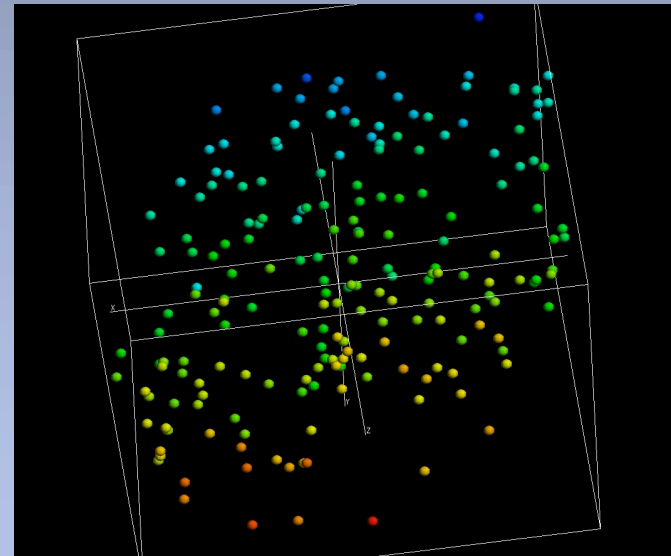
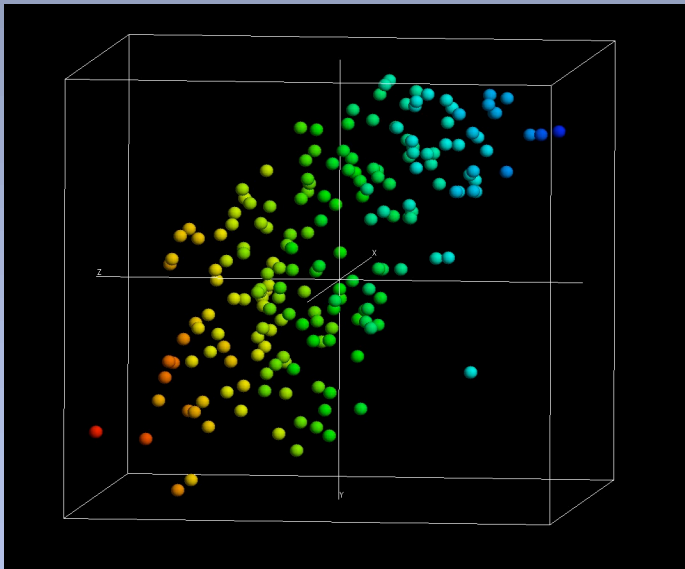
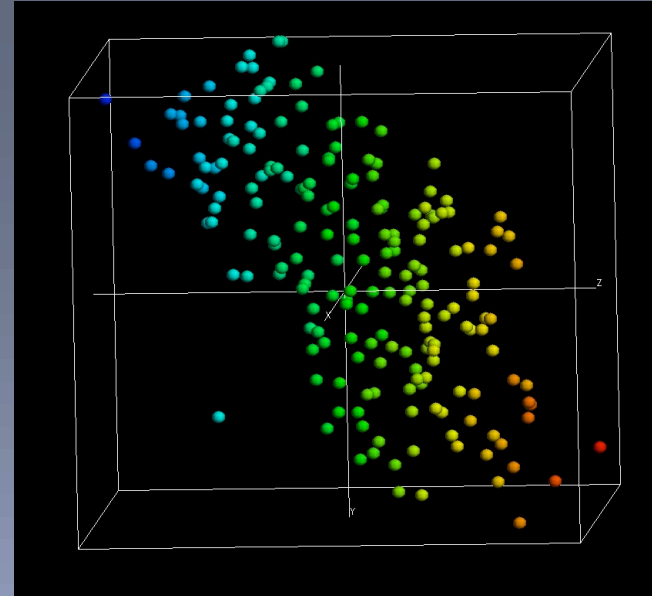
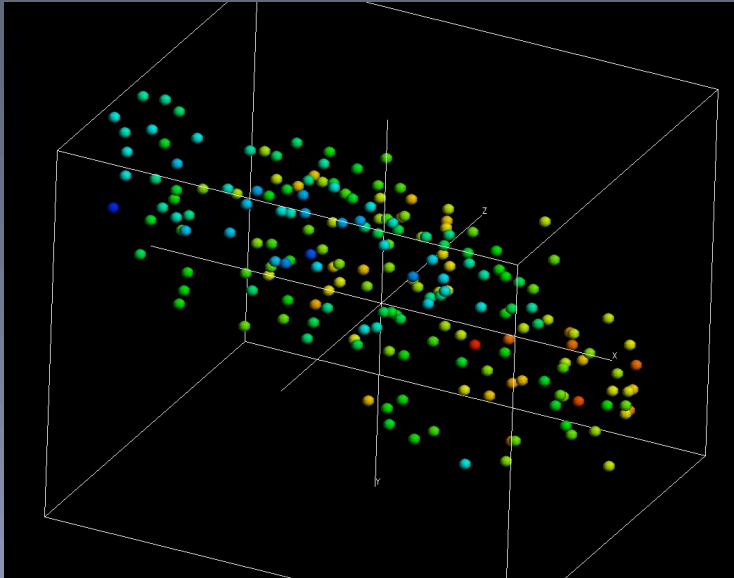


*Planar structure !*



A more complex flock

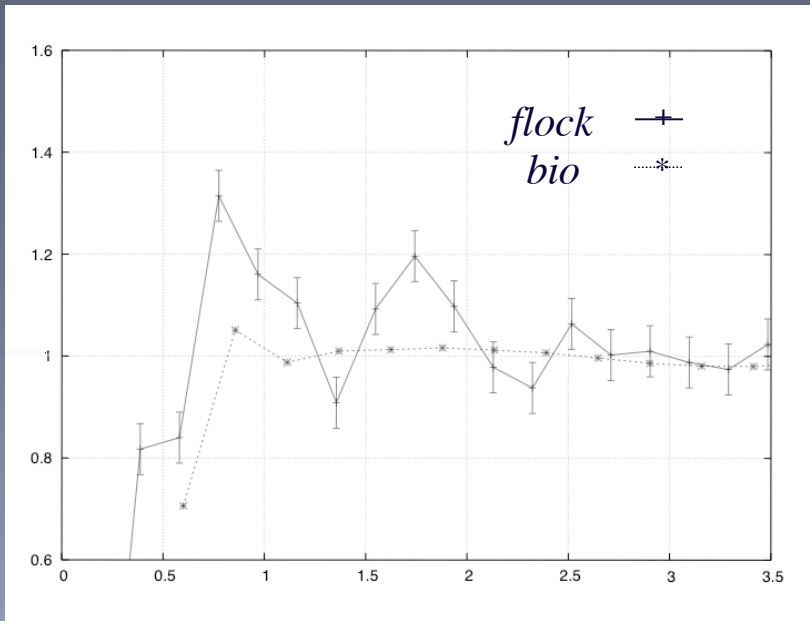




Discoidal shape



$g(r)$

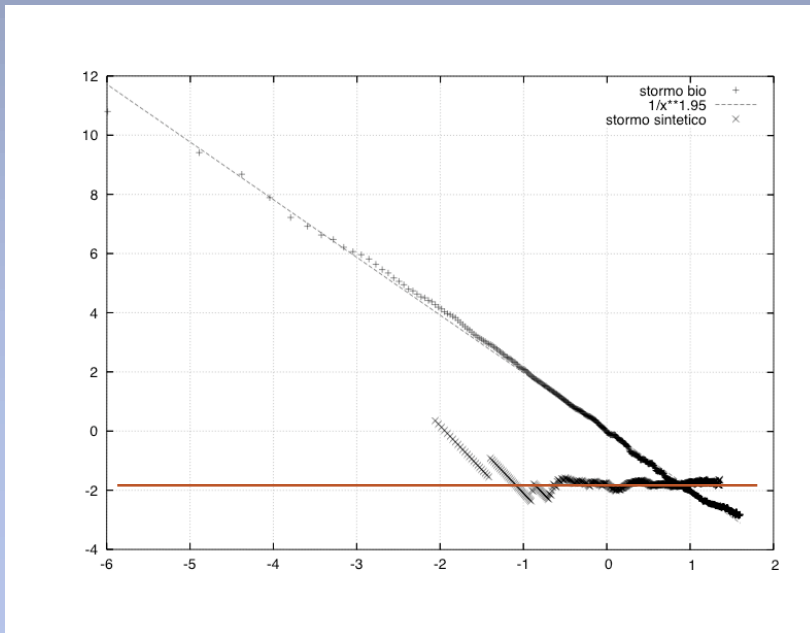


Radial distribution function  $g(r)$

Liquid like !!!

$r$

$\Gamma(r)$



Conditional mass  $\Gamma(r)$

Scale free (???)

*very preliminary*

Finite size effect ( $L < L^*$ )

Errors in segmentation

Errors in matching ?

Density =  $N/V$

← Synthetic flock with same  $V$ ,  $N$  and overall shape as the bio one, but with a uniform distribution of points

$r$

## Summary and Perspectives



- 3D reconstruction of starling flocks is demanding but possible
- Experimental efficiency related to  
Camera specifications (Canon Eos D Mark II, 8.2 Mp, 8.5 fps)  
alignment capabilities
- Static reconstruction of individual flocks

- Statistics → correlation functions, shape, heterogeneity
- Dynamics → trajectory reconstruction, diffusion, convection

Comparison with models

# The team

## ***Alberto Orlandi***

(INFM-CNR, **STARFLAG** postdoc)  
computer vision, epipolar geometry

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***Giorgio Parisi*** (La Sapienza, INFM & ISC)